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2 **Einstein's 1905 'Annus Mirabilis': Reconciliation of the Basic**
3 **Research Traditions of Classical Physics**

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7 **Abstract**

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9 together one has to take into consideration Einstein's strive for unity evinced in his
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24 knowledge · Mach · Stevinus · Constructive theory · Kant

25 **1 Introduction**

26 It is a commonplace idea that Einstein's scientific contributions were highly moti-
27 vated by the ideal of unity of physical laws, and this had a considerable influence
28 on the whole theoretical physics community (see, for instance, van Dongen 2010).
29 For example in the 1949 epoch-making Schilpp volume Einstein, reflecting on his

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30 scientific creativity in general, eagerly acknowledged that “the special aim which
31 I have *constantly* kept before me is *logical unification* in the field of physics” (Ein-
32 stein 1949a, p. 400; my italics).

33 And it is well-known that all the scientific career of Einstein after 1915, i.e. after
34 the general relativity had been achieved, was precisely the vehement search for uni-
35 tary theories, unification of gravitation and electrodynamics, and so on (see, for
36 instance, Vizgin 2011). And it is no wonder that the quest for unity of nature is best
37 illustrated by *these* attempts of Einstein towards unitary theories during almost forty
38 years than by the early works.

39 Yet, in my innermost conviction, Einstein’s mature unification efforts and espe-
40 cially his stupendous general relativity had sprung out of his early writings and first
41 and foremost out of his 1905 obstinate efforts to create special theory of relativity,
42 as well as out of his audacious 1905 light quanta hypothesis. For instance, as Ein-
43 stein recalled later, his strenuous efforts to set up the basic general relativity tenet—
44 the principle of equivalence—were drawn upon his experience of creating the SRT
45 (special relativity theory):

46 At this point, there occurred to me the happiest thought in my life [der glück-
47 lichste Gedanke meines Lebens]. *Just as in the case with the electric field* pro-
48 duced by electromagnetic induction, the gravitational field has similarly only
49 a relative existence. For if one considers an observer in free fall, e.g. from the
50 roof of a house, there exists for him during this fall no gravitational field – at
51 least not in his immediate vicinity. Indeed, if the observer drops some bodies,
52 then these remain relative to him in a state of rest or in uniform motion, inde-
53 pendent of their particular chemical or physical nature (quoted from Pais 1982,
54 p. 178; my italics).

55 Likewise, his revolutionary 1905a paper on light quanta starts with unfolding “a
56 *profound formal difference* between the theoretical conceptions physicists have
57 formed about gases and other ponderable bodies and Maxwell’s theory of elec-
58 tromagnetic processes in so-called empty space” (Einstein 1905a, p. 86, my bold
59 italics). The paper as a whole aims at unification of the basic research traditions of
60 classical physics. Moreover, Einstein’s 1905d paper on special relativity commences
61 with scrutinizing a “*deep asymmetry*” (Einstein 1905d, p. 140) in the electromag-
62 netic induction description. Furthermore, as Einstein recalled later in his fascinating
63 “*Evolution of Physics*”,

64 The relativity theory arose from necessity, from *serious and deep contradic-*
65 *tions* in the old theory from which there seemed no escape. The strength of the
66 new theory lies in the *consistency* and *simplicity* with which it solves all these
67 difficulties, using only a few convincing assumptions.

68 Although the theory arose from the field problem, it has to embrace all physi-
69 cal laws. A difficulty seems to appear here. The field laws on the one hand and
70 the mechanical laws on the other are of *quite different kinds*. The equations of
71 electromagnetic field are invariant with respect to Lorentz transformations and
72 the mechanical equations are invariant with respect to the classical transforma-
73 tions (Einstein and Infeld 1938, p. 202; my italics).

74 Hence *the overall aim of the present paper is to take the next step and to unfold the*
75 *abiding influence of unification on Einstein's 1905 papers and especially on SRT*
76 *genesis and advancement.* Accordingly, the next part of this paper deals with the cir-
77 cle of unification problems that brought Einstein to electrodynamics of moving bod-
78 ies. The aim of the third part is to answer the question: what was the train of thought
79 that provoked Einstein to invent light quanta and SRT. It is argued that the former
80 and the latter turn out to be mere milestones of implementation of maxwellian elec-
81 trodynamics, statistical mechanics and thermodynamics reconciliation programme.
82 The leading part in the programme was played by Einstein's 1905a light quanta
83 paper, since it was first and foremost the ether conception that put insurmountable
84 obstacles in realization of Einstein's statistical-thermodynamics design. Finally, my
85 ultimate aim will be to exhibit that the pivotal concept necessary to conceive Ein-
86 stein's relativity creation and all his 1905 papers *as a whole*, as well as the *order* of
87 their arrangement is Mach's principle of Economy of Thought taken in the context
88 of his 'instinctive knowledge' principle and with some faint inclinations of Kantian
89 epistemology presuming the coincidence of both constructing theory and integrating
90 intuition of Principle.

91 **2 Einstein, Helmholtz, Hertz, Poincaré, Hume and Mach**

92 In Germany Maxwell's strenuous efforts to arrive at a reasonable compromise
93 between the research programmes of Young–Fresnel, Faraday and Ampère–Weber
94 (Nugayev 2015) were set forth by Hermann Helmholtz and his star pupil Heinrich
95 Hertz. In Helmholtz's seminal paradigm (Helmholtz 1870) charges and currents
96 were taken as the sources of electrical and magnetic fields. It led directly to H.A.
97 Lorentz's dualistic worldview of the field equations and the equations of motion
98 exhibited in his 1892–1900 papers. Lorentz's theory was an ingenious amalgamation
99 of Maxwell's field theory and Wilhelm Weber's particle theory of electrodynamics.

100 And it was young Albert Einstein who dared to pick up the problem after Max-
101 well, Helmholtz, Hertz and Lorentz. In early August 1899 letter to Mileva Marić an
102 ETH (Eidgenössische Technische Hochschule) student acknowledges that "I admire
103 the original, free mind of Helmholtz more and more"(Doc. № 50 of Einstein 1987,
104 129). In 10 August 1899 'Paradies' hotel letter he confesses to his fiancée that

105 I am more and more convinced that the electrodynamics of moving bodies, as
106 presented today, is not correct, and that it should be possible to present it in a
107 simpler way. The introduction of the term 'ether' into the theories of electricity
108 led to the notion of a medium of whose motion one can speak without being
109 able, I believe, to associate a physical meaning with this statement. I think that
110 the electric forces can be directly defined only for empty space, which is also
111 emphasized by Hertz [...]

112 Electrodynamics would then be the theory of the motion of moving electrici-
113 ties and magnetisms in free space: which of the two conceptions must be cho-
114 sen will have to be revealed by radiation experiments (Doc. № 52 of Einstein
115 1987, p. 131).

116 It was Hertz's fine 1890 paper "*Über die Grundgleichungen der Elektrodynamik*
117 *für bewegter Körper*" ("On the Basic Equations of the Electrodynamics of Moving
118 *Bodies*") that appeared to be the source of the phrase "*bewegter die Elektrodynamik*
119 *Körper*" ("Electrodynamics of Moving Bodies") in the heading of Einstein's 1905d
120 STR paper. Einstein used these words in the letter and thereafter to designate the
121 complex of problems that eventually led him to special relativity. Nevertheless, Ein-
122 stein was not a slavish adherent of Hertz's "*Darstellung*" (representation). From the
123 very beginning of his scientific career Einstein had persistently expressed doubts on
124 the role of 'des Namens Aether' (of the name Aether) in electrodynamics. Yet his
125 skepticism was directed at Hertz's concept of the ether as *a medium with a certain*
126 *state of motion*, not at the ether concept *itself*. It was because Einstein attributed
127 basic significance to the concept of 'elektrische Massen' (electrical masses) and
128 treated electric currents as real motions of such charges in empty space, and not as
129 the 'Verschwinden elektrische Polarisation in der Zeit' (missing electrical polarisa-
130 tion in space). At the start of Einstein's scientific career his views were drawn upon
131 the lectures on electricity of his ETH physics teacher prof. H.F. Weber, as is indi-
132 cated by Einstein's lecture notes (see, for instance, Doc. № 37 and salient comments
133 on it in Einstein 1987, pp. 223–225).

134 The 'substantive' concept of electricity was advanced by Wilhelm Weber and
135 was widely accepted by many German-speaking physicists, including H.F. Weber.
136 Therein, *initially Einstein's views on electrical masses moving in the immobile ether*
137 *were similar to the dualistic theory of H.A. Lorentz*. Einstein concluded the above-
138 mentioned letter recapitulating that 'Strahlungsversuche' (radiation experiment) was
139 necessary for choosing between the two viewpoints he outlined, and his next, 10
140 September 1899 'Paradise' letter to Marić judiciously mentioned an idea for experi-
141 mentally investigating the influence of motion relative to the ether on light propaga-
142 tion in transparent bodies.

143 Though, Einstein's physics professor manifested no enthusiasm for his work, and
144 Albert made no further mention in his correspondence of his activity in the electro-
145 dynamics of moving bodies for almost two years. Nevertheless 'die prinzipielle
146 Trennung von Lichtaether und Materie' (the principal separation of light aether and
147 matter), 'Definition absoluter Ruhe' (definition of absolute rest), etc. were among
148 the topics he vividly discussed with his close friend Michele Besso (see Einstein's
149 4 April 1901 letter to Marić). In March 1901 Einstein informed Miss Marić that
150 he looked forward to the conclusion of "*unsere Arbeit über die Relativbewegung*"
151 (our work on relative motion). In September 1901 he informed his boon compan-
152 ion Marcel Grossman on inventing a simpler method for the investigation of the
153 motion of matter relative to ether, based 'auf gewonlichen Interferenzversuchen' (on
154 customary interference experiments). By December 1901 he was 'arbeite eifrigst'
155 (working hard) on "*die Elektrodynamik bewegter Körper*" (the electrodynamics of
156 moving bodies), that promised to become "eine kapitale Abhandlung" (a capital treatise)
157 (Einstein's 17 December 1901 letter to Marić). A calculation error had earlier
158 led him to doubt the correctness of his 'Ideen über die Relativbewegung' (ideas on
159 relative motion), but he now believed in these ideas more than ever. He unfolded
160 the motley stuff to prof. Kleiner and the latter even "thought that the experimental
161 method proposed by me is the simplest and most appropriate and conceivable. I was

162 very pleased with the success. I shall certainly write the paper in the coming weeks”
163 (Einstein’s letter to Marić, 19 December 1901, p. 189). Notwithstanding prof. Klein-
164 er’s encouragement and Einstein’s youthful enthusiasm, no publication on this sub-
165 ject ensued for over three years—till 21 June 1905.—Why? What was the matter?—
166 Einstein really was working hard on a “capital treatise” on the electrodynamics of
167 moving bodies at the end of 1901. Then he had desisted and retraced to the memoir
168 only in 1905. What did happen in that span, and *why had Einstein, being initially*
169 *an adherent of the ether, became its strong enemy?*

170 To give a sober answer one has first to recall Einstein’s derogative evaluation
171 of his early works—‘my worthless beginner papers’ (Einstein/Marić 1992). All
172 the evidence at hand indicates that the planned “*kapitale Abhandlung*” was a ‘far
173 cry’ from the 1905d preeminent STR paper. On the other hand, now one knows
174 for sure (Rynasiewicz 2000) that Einstein arrived at the body of results presented
175 in his 1905d relativity paper, in a ‘sudden burst of creativity’ and only after he
176 had completed his first three works in the spring of 1905. *The key insight—the*
177 *discovery of the relativity of simultaneity—occurred to Einstein only in late May*
178 *1905 after the completion of the 1905c Brownian motion paper.* For instance,
179 when asked by the biographer Carl Seelig, Einstein enunciated:

180 Between the conception of the idea of the special theory of relativity and
181 the completion of the corresponding published paper there passed five or six
182 weeks (Seelig 1960, p. 114).

183 Maybe Einstein had renounced the ether concept on finding some uncontest-
184 able, irrefutable *physical* argument in the writings of those luminaries of science
185 whose influence he readily and publicly admitted? The argument could turn out a
186 final straw for growing aversion to ostensible metaphysical remnant of the obso-
187 lete classical research traditions.

188 To begin with, how important was Poincaré and Mach’s proverbial influ-
189 ence?—Indeed, in a letter to Michele Besso on 6 March 1902 Einstein recalled:

190 These readings were of considerable influence on my development – along
191 with Poincaré and Mach (Speziali 1972, Doc. 182).

192 At first, how crucial was Poincaré’s pre-eminent ‘Relativity Principle’, that
193 asserted relativity of time and space? Already in 1902 Henri Poincaré contended
194 that

195 *There is no absolute time.* To say two durations are equal is an assertion
196 which has by itself no meaning and which can acquire one only by con-
197 vention. Not only have we no direct intuition of the equality of two dura-
198 tions, but *we have not even direct intuition of the simultaneity of two events*
199 *occurring in different places:* this I have explained in an article entitled ‘*La*
200 *mesure du temps*’ (Poincaré 1902, p. 114; my italics).

201 Furthermore, one of droll ‘Academia Olympia’ members—Einstein’s close friend
202 Maurice Solovine—took Henri Poincaré’s book “*La science et l’hypothese*” (first
203 published in 1902) as one

204 that profoundly impressed us and kept us breathless for many weeks (Solovine
205 1956; quoted from Howard and Stachel 2000, p. 6).

206 Nevertheless, *the relativity principle, elaborated by Henri Poincaré, did not prevent*
207 *the latter from believing in luminiferous ether* as in the medium necessary for propa-
208 gation of electromagnetic disturbances (Darrigol 2001).

209 And as for Ernst Mach, in a letter of 8 April 1952 to Carl Seelig, Einstein
210 confessed:

211 My attention was drawn to Ernst Mach's '*Science of Mechanics*' by my friend
212 Besso while a student, *around the year 1897*. The book exerted a *deep and*
213 *persisting* impression upon me owing to its *physical* orientation toward funda-
214 mental concepts and fundamental laws (quoted from Holton 1968, p. 636; my
215 italics).

216 The apparent influence on Einstein of Mach's critique of Newton's concepts of
217 absolute space and absolute time is a humdrum. For instance, according to Mach's
218 famous dictum

219 It is scarcely necessary to remark that in the reflections here presented Newton
220 has again acted contrary to his expressed intention only to investigate *actual*
221 *facts*. No one is competent to predicate things about absolute space and abso-
222 lute motion; they are pure things of thought, pure mental constructs, that *can-*
223 *not be produced in experience*. All our principles of mechanics are, as we have
224 shown in detail, experimental knowledge concerning the *relative* positions and
225 motions of bodies (Mach 1893/1999, p. 229; my italics).

226 On the other hand, in 1916 Einstein himself asserted:

227 I can say *with certainty* that the study of Mach and Hume has been directly a
228 *great help* in my work...Mach recognized the weak spots of classical mechan-
229 ics and was not very far from requiring a general theory of relativity half a
230 century ago... (quoted from Frank 1949, p. 272; my bold italics).

231 Yet, of course, there is apparently no direct and unambiguous way from elevated
232 philosophical critique of Newtonian mechanics to queer postulates of special rela-
233 tivity (see, for instance, Zahar's startling 1973 account). It should be added that the
234 strongest argument against the inductivist explanation of the STR genesis consists in
235 the following. Let us turn to the so-called "emission theories of light" that contested
236 the light-constancy postulate and exchanged it with the Galilean law (that simply
237 added the velocities of light and of its source). These theories (see Tolman 1912 for
238 details) had *no* problems in explaining the Michelson–Morley result since they were
239 specially conjured up to explain it. And they did. But they should not, if the induc-
240 tivists were right.

241 One can, of course, appeal to falsificationist explanation, contending that the
242 Lorentz–Fitzgerald contraction (LFC) hypothesis, aimed at explaining the Michel-
243 son–Morley results within the classical physics research tradition, was an "ad hoc"
244 hypothesis. Indeed, presumably following Poincaré's lecture (Rapports du Congrès
245 de Physique de 1900, Paris, i, pp. 22–23), Einstein in his 1907 exposition of the

246 STR characterized Lorentz's and Fitzgerald's contraction hypothesis as an "ad hoc"
247 one and "only an artificial means of saving the theory" from the negative results of
248 Michelson and Morley 1887 experiment. However, in his subsequent writings Poin-
249 caré, starting from his eminent St. Louis lecture (1904), had irrevocably changed
250 his mind. Correspondingly, Einstein did not label the LFC hypothesis as 'ad hoc'
251 anymore.

252 Yet it is Elie Zahar's (1973) conspicuous account of ad hocness in the context
253 of the Lorentz–Einstein transition that had convincingly exhibited that the Lor-
254 entz–Fitzgerald contraction hypothesis was not an ad hoc_i (i=1,2,3) hypothesis.
255 According to Zahar, the most complete and multifarious account of ad hocness
256 in philosophy of science is provided by Imre Lakatos's methodology of scientific
257 research programmes.

258 A theory is said to be ad hoc₁ if it has no novel consequences as compared
259 with its predecessor. It is ad hoc₂ if none of its novel predictions have been
260 actually 'verified'; for one reason or another the experiment in question may
261 not have been carried out, or - much worse - an experiment devised to test a
262 novel prediction may have yielded a negative result. Finally the theory is said
263 to be ad hoc₃ if it is obtained from its predecessor through a modification of
264 the auxiliary hypothesis which does not accord with the spirit of the heuristic
265 of the programme (Zahar 1973, p. 217).

266 Zahar convincingly exhibited that the Lorentz–Fitzgerald contraction hypothesis
267 was not an ad hoc₁ one evidently because the STR and the LFC predicted *different*
268 results of the Kennedy–Thorndike experiment. Likewise, LFC was not an ad hoc₃
269 hypothesis too. Lorentz derived the LFC hypothesis from a *deeper* theory—from
270 the Molecular Forces Hypothesis (MFH): "molecular forces transform and behave
271 like electromagnetic ones". It was quite natural for Lorentz to admit that there is no
272 special "molecular" ether to transmit the interactions between the bodies. All the
273 interactions should be transmitted by the common "luminiferous" ether.

274 It is also necessary to supplement that, while Zahar correctly takes the LFC
275 hypothesis as non ad hoc₂, his sophisticated arguments are rather doubtful since they
276 are grounded on his notorious 'definition of the novel fact'.

277 A fact will be considered novel with respect to a given hypothesis if it did
278 not belong to the problem situation which governed the construction of the
279 hypothesis (Zahar 1973, p. 218).

280 I approve Alan Musgrave (1974, pp. 13–14) in that Zahar's definition is rather dubi-
281 ous since it puts the procedures of empirical justification from the hands of experi-
282 mentalists to the hands of historians of science. Such a comprehension of the novel
283 fact deviates as a matter of fact from Lakatosian "temporal novelty". On my humble
284 opinion Zahar's redefinition of the novel fact is redundant for the defence of the LFC
285 hypothesis. As a matter of fact LFC is not an ad hoc₂, but due to the other fine rea-
286 sons. The following quotation is of importance here:

287 This assumption of a shrinkage, although bold and thus far entirely hypotheti-
288 cal, is not impossible and is the only suggestion yet made which is capable of
289 reconciling the negative results of second and third order experiments with a
290 quiescent ether. Poincaré (Rapports du Congrès de Physique de 1900, Paris,
291 i, pp. 22–23) has raised objection to the electromagnetic theory for moving
292 bodies, that each time new facts are brought to light a new hypothesis has to
293 be introduced. This criticism seems to have been fairly met by Lorentz in his
294 latest treatment of this subject (Brace 1905, p. 72).

295 Advancing Lorentz's arguments, Brace skillfully employed the results of Hasenörl
296 (Annalen der Physik, 1903, band 13, p. 367). Reasoning from a cyclic process in
297 a moving radiating system, Hasenörl had elicited that the second law of thermo-
298 dynamics is blatantly contradicted unless a second order contraction takes place.
299 Hence not only the Michelson–Morley experiment, but *all* the variety of the experi-
300 ments establishing the second law of thermodynamics support the LFC. This is an
301 outstanding empirical confirmation!

302 In the upshot, Einstein carefully and zealously perused Mach's "*Science of*
303 *Mechanics*" already in 1897; yet this did not hamper to him to believe in luminifer-
304 ous ether up to 1905.

305 Or maybe it was sage David Hume? For instance, in a letter to Michele Besso in
306 1948 Einstein again recalled that

307 How far [Mach's writings] influenced my own work is, to be honest, not clear
308 to me. In so far as I can be aware, the *immediate* influence of D. Hume on me
309 was great. I read him with Konrad Habicht and Solovine in Bern (quoted from
310 *Speziali* 1972, p. 153; my italics).

311 Yet it should be stressed that Hume's and Einstein's conceptions of space and time
312 have *substantial* differences (see Slavov 2016 for details). In Hume's adamant epis-
313 temological doctrine, space and time are *direct* abstractions from simple percep-
314 tions. On the contrary, Einstein stubbornly and constantly emphasized that the basic
315 concepts of science are *free creations* of the human mind (see, for instance, Schil-
316 pp's 1949 eminent volume and all the references cited therein).

317 **3 What was the Train of Thought that Brought Einstein to Special** 318 **Relativity?**

319 To give a reasonable and cogent answer one should first delve into the special rela-
320 tivity paper itself (Einstein 1905d). The paper famously commences with scrutiniz-
321 ing a "*deep asymmetry*" in the description of electromagnetic induction. Experience
322 tells us that the induction current caused in the conductor by the motion of the mag-
323 net depends only on *relative* motion of the conductor and the magnet. However the
324 Maxwell–Lorentz theory provides one with *two* qualitatively different accounts of
325 the effect that mysteriously lead to one and the same quantitative result.

326 But for conceiving the sober reasons of special relativity genesis it is quite
327 important to take into consideration that *Albert Einstein was by no means the*

328 *first to note asymmetries in theoretical representation of the induction phenom-*
329 *enon*. In 1885 the asymmetries were indicated by Oliver Heaviside, in 1894—by
330 Herman Föppl, and in 1898—by Wilhelm Wien himself (see Darrigol 2001, p.
331 377 for details). One should especially punctuate Heinrich Hertz’s thought-pro-
332 voking papers. For instance, Hertz explicitly used the term ‘asymmetry’ in his
333 1884 paper. Hence it is no wonder that namely Hertz’s papers constituted part
334 of the background to Einstein’s thinking on issues in electrodynamics (Hon and
335 Goldstein 2005). Really, at the outset of his 1905d paper Einstein invoked Max-
336 well’s equations in their Hertzian form, namely, in the symmetrical form that
337 Hertz presented for the first time in his 1884 paper. In his 1905d STR paper Ein-
338 stein is explicit about this: he appeals to the “Maxwell–Hertz” equations. How-
339 ever, Hertz took this asymmetry as purely formal, and he easily eliminated it by
340 re-writing Maxwell’s equations in a symmetrical form.

341 Thus the pivotal question is not how Einstein became aware of the asymmetries,
342 but *what made them so intolerable to him*. Einstein followed Hertz, Heaviside,
343 Wien et al. in recognition that something was pathological in the Maxwell–Lorentz
344 theory. Yet he had to provide a rather manifold ‘diagnosis’ and to choose a peculiar
345 ‘cure’.

346 The key to answer the aforementioned question lies in *other* works of Albert Ein-
347 stein and first and foremost in his papers of 1905. It is well-known that Einstein
348 published *nothing* on the topic of optics and electrodynamics of moving bodies prior
349 to 1905. Moreover, it was Albert Einstein himself who had just disclosed *another*
350 *asymmetry—and of more profound nature*—in the 1905a paper “*On an heuristical*
351 *point of view concerning the processes of emission and transformation of light*” that
352 was published in the same journal “*Annalen der Physik*” but three months *before* the
353 relativity paper. Behold the outset of his 1905a ground-breaking paper:

354 There exists *a profound formal difference* between the theoretical conceptions
355 physicists have formed about gases and other ponderable bodies and Max-
356 well’s theory of electromagnetic processes in so-called empty space (Einstein
357 1905a, p. 86, my bold italics).

358 And in the first part of the trailblazing paper Einstein excavates that *joint* appli-
359 cation of mechanical and electrodynamic “theoretical pictures” for scrutinizing the
360 black-body radiation leads not only to the crying contradictions with experiment (his
361 paper did not even cite Lummer and Pringsheim or Rubens and Curlbaum results),
362 but to the startling *paradox* that cannot be circumvented by common expedients and
363 evasions. To exhibit it, Einstein contrives the gedankenexperiment with the both
364 theories. He contemplates an imaginary cavity containing free electromagnetic field,
365 gas molecules and Hertz’s resonators. In the sequel he arrives at a conclusion that
366 the joint application of mechanics and electrodynamics leads *unavoidably* to Ray-
367 leigh–Jeans law for energy density of the black-body radiation. However,

368 “this relation which we found as the condition for dynamic equilibrium does
369 not only lack agreement with experiment, but it also shows that in our picture
370 there can be no question of a definite distribution of energy between aether and
371 matter”, since “the greater we choose the range of frequencies of resona-

372 tors, the greater becomes the radiation energy in space and in the limit we get
373 $\int_0^\infty \rho_\nu d\nu = (R/N)(8\pi/L^3)T \int_0^\infty \nu^2 \rho_\nu d\nu = \infty.$ "

374 (Here R denotes the universal gas constant, N the number of "real molecules" in
375 one gram-equivalent, T the absolute temperature, L the velocity of light, ν the fre-
376 quency, and $\rho_\nu d\nu$ the energy per unit volume of that part of the radiation whose
377 frequency lies between ν and $\nu + d\nu$).

378 Although it is commonly held that in the 1905a paper Einstein was concerned
379 with an explanation of the photoelectric effect, the tentative study of the master-
380 piece discloses that this was not the case. The measurements of the effect at that
381 time were not sufficiently accurate to point without any doubt to a violation of clas-
382 sical behavior (see Ter Haar 1967 for details). Einstein was worried not so much by
383 the evidence dealing with photoeffect and appealed to fluorescence, photoelectricity
384 and photoionization data only as to *indirect* evidence in favor of his thesis. Rather,
385 Einstein had mostly delved into the contemplation of the profound *contradiction*
386 between mechanics and electrodynamics and to the efficacious ways of resolving it.

387 So, ***what was a judicious reason of Einstein's deep interest to the contradic-***
388 ***tions*** between the mature physical theories?

389 I think that to find a weighty answer one has to turn to Einstein's 1946 'Auto-
390 biographical Notes' once more:

391 It was Ernst Mach who, in his History of Mechanics, shook this dogmatic
392 faith; this book exercised a *profound influence* upon me in this regard while I
393 was a student. I see Mach's greatness in his *incorruptible skepticism* and inde-
394 pendence; ***in my younger years, however, Mach's epistemological position***
395 ***also influenced me greatly...*** (Einstein 1949a, p. 21; my bold italics).

396 Now it is clear why Tetu Hirosgie (1976) shrewdly attributed Einstein's sensi-
397 tivity to the inconsistencies between mechanics and electrodynamics to abid-
398 ing influence of Ernst Mach, whose writings supposedly helped the inventor of
399 special relativity to outdo the dogmatic adherence to the mechanistic worldview.
400 Mach's "*Science of Mechanics*" is teeming with vehement attacks against classi-
401 cal mechanics imperious role in physics. For instance,

402 The view that makes mechanics *the basis* of the remaining branches of phys-
403 ics, and explains all physical phenomena by mechanical ideas, is in our judge-
404 ment a *prejudice*. Knowledge which is historically first, is not necessarily the
405 foundation of all that is subsequently gained. As more and more facts are dis-
406 covered and classified, entirely new ideas of general scope can be formed. We
407 have no means of knowing, as yet, which of the physical phenomena go *deep-*
408 *est*, whether the mechanical phenomena are perhaps not the most superficial of
409 all, or whether all do not go equally deep.[...] The science of mechanics does
410 not comprise the foundations, no, nor even a part of the world, but only an
411 *aspect* of it (Mach 1893/1999, pp. 495, 517; my italics).

412 Einstein could therefore freely and playfully juxtapose Newtonian mechanics,
413 Maxwellian electrodynamics and statistical thermodynamics without reducing
414 one to the others.

415 Renn and Schulmann (1992) take Einstein's anti-dogmatism as a crucial hall-
416 mark of his scientific style of reasoning that enabled a young man to comprehend
417 the conceptual implications in the works of such masters as Lorentz, Hertz, Poin-
418 caré and Planck that they themselves were sometimes unable to discern.

419 Yet the crucial element of Machian epistemology that persistently accompa-
420 nied Einstein's creativity beginning from 1897 and till his last days was Mach's
421 famous Principle of Economy of Thought: "Physics is Experience Arranged in
422 Economical Order" (Mach 1897/1984).

423 Mach commences his "*Science of Mechanics*" by maintaining that "Economy
424 of communication and of apprehension is of the very essence of science" (Mach
425 1893/1999, p. 6). And through and through the whole book the principle is stub-
426 bornly and constantly applied to various physical epistemological and philosphi-
427 cal problems, so that "This economical office of science, which fills its whole life,
428 is apparent at first glance, and with it full recognition all mysticism in science
429 disappears" (Mach 1893/1999, p. 481).

430 Accordingly, in his review of STR genesis, published in "*Science*" in 1940,
431 Einstein directly acknowledges that "the theory of relativity arose out of efforts to
432 improve, with reference to *logical economy*, the foundation of physics as it existed
433 at the turn of the century" (Einstein 1940/1954, p. 329; my italics. See also Einstein
434 1933/1954, p. 277; Einstein 1936/1954, p. 293 and Einstein 1944/1954, p. 23).

435 And a judicious explanation of Einstein's reasons for arriving at his 1905a
436 paper and its connections with the other 1905 ones can be found again in his
437 "*Autobiographical Notes*". According to Einstein, the first stage of "the revolu-
438 tion begun by the introduction of the field" (Einstein 1949a, p. 37) consisted in
439 the invention and in the consolidation of the Maxwellian electrodynamics. All
440 the pre-maxwellian accounts of physical interactions (the pre-eminent theories of
441 Newton, Ampère, Weber, Riemann et al.) were theories of interactions between
442 several *material points*. Owing to Faraday and Maxwell, the *Electromagnetic*
443 *Field* was thrust into the texture of the nineteenth century physics as a steadfast
444 element of physical reality having equal rights with the *Material Point*. The prob-
445 lem situation was characterized by

446 the dualism which lies in the fact that the material point in Newton's sense
447 and the field as continuum are used as elementary concepts *side by side*.
448 Kinetic energy and field-energy appear as *essentially* different things (ibid,
449 p. 37; my italics).

450 Correspondingly, as an inevitable consequence of the dualism

451 a "fundamental crisis set in, the seriousness of which was suddenly recog-
452 nized due to Max Planck's investigations into heat radiation (1900). The
453 history of this event is all the more remarkable because, at least in its first
454 phase, *it was not in any way influenced by any surprising discoveries of an*
455 *experimental nature*" (ibid, p. 37; my italics).

456 Max Planck's form of reasoning [$\varepsilon = h\nu$] apparently contradicted the mechani-
457 cal and electrodynamical basis upon which his derivation depended. Yet it should
458 be stressed that

459 My own interest in those years was less concerned with the detailed conse-
460 quences of Planck's results, however important these might be. My major
461 interest was: What general conclusions can be drawn from the radiation for-
462 mula ... concerning the structure of radiation *and even more concerning the*
463 *electro-magnetic foundations of physics?* (Einstein 1949a, p. 47; my italics).

464 Thus Einstein's attraction in the 1905a paper to the subject of theory of quanta was
465 provoked by its *unifying possibilities*, for its capacities to arrive at a successful
466 *fusion* of Maxwellian electrodynamics and Boltzmann's statistical thermodynamics.
467 Hence he starts the paper with the heart of what troubled him most—the Rift, *the*
468 *Duality* in the foundations of physics that was felt most sharply in Lorentz's Elec-
469 tron Theory (and "H. A. Lorentz knew this very well"; Einstein 1949a, 37). ***How did***
470 ***Einstein intend to eliminate the pivotal contradiction of his 1905a paper?***

471 While considering Einstein's way out of the predicament, one should take into
472 account that *all* Einstein's papers from 1901 to 1905 have one trait in common:
473 statistical-thermodynamics approach. Thomas S. Kuhn had punctuated that *what*
474 *brought Einstein to idea of photon was a coherent development of a research pro-*
475 *gram started in 1902*, a program "so nearly independent of Planck that it would
476 almost certainly have led to the black-body law even if Planck had never lived"
477 (Kuhn 1978, p. 171). From the outset of his scientific career Einstein was "deeply
478 impressed" (Martin Klein) by the simplicity and scope of classical thermodynamics.
479 But for him thermodynamics included the statistical approach he had imbibed from
480 Boltzmann's works, and so he started to unfold statistical thermodynamics. The
481 result was a series of three papers published in 1902, 1903 and 1904. It should be
482 stressed that expressly *they provide the clue for apprehending his 1905a paper on*
483 *quanta, his 1905b dissertation, 1905c work on Brownian motion and 1905d paper*
484 *on special relativity.*

485 The first important result consisted in that for physical systems of extraordi-
486 nary general sort Einstein had produced, by the summer of 1903, both a general-
487 ized measure for temperature T and entropy S , containing some universal constant
488 χ . By the time he finished his 1903 paper, Einstein had recognized that χ could be
489 evaluated in terms of the values of the gas constant and of Avogadro's number. But
490 the theory that had led him to the constant was, however, applicable to systems far
491 more general than gases. It should therefore have a correspondingly general physical
492 foundation. The basis should reflect statistical-mechanical nature of the approach
493 that led him to the constant, explaining not only its role as a scale factor for tempera-
494 ture, but also its position as a multiplier in the probabilistic definition of entropy.
495 Physical significance of χ was the central problem attacked in Einstein's third statis-
496 tical paper "*On the General Molecular Theory of Heat*", submitted to the "*Annalen*"
497 in the spring of 1904. The solution of the problem consisted in the phenomena of
498 energy fluctuations. Einstein elucidated that $\bar{\varepsilon}^2 = 2\chi T dE/dT$, where $\bar{\varepsilon}^2$ is a measure
499 of thermal stability of the system, T —temperature of the system and E its energy.

500 And it was comprehension of the constant physical sense that directed his attention
501 to the black-body problem.

502 The equation just found would permit an exact determination of the universal
503 constant χ if it were possible to determine the energy fluctuation of the system.
504 In the present state of our knowledge, however, that is not the case. Indeed,
505 for only one sort of physical system can we presume from experience that an
506 energy fluctuation occurs. That system is empty space filled with thermal radi-
507 ation (Einstein 1904, p. 360]; translated in Kuhn 1978).

508 At least one more step in the programme of statistical thermodynamics advance-
509 ment was needed, and Einstein took it in the ground-breaking 1905a paper. Its con-
510 tent suggests that Einstein had begun to seek a black-body law of his own, and that
511 he had quickly encountered the paradox, evinced in the contradiction between sta-
512 tistical mechanics and maxwellian electrodynamics, and that he had opportunely
513 dropped the search for the law in favour of an exploration of the paradox itself. This
514 is clear from the very beginning of his already quoted paper (translated in Ter Haar
515 1967). The first part of the 1905a paper came to an end by revelation of the “ultra-
516 violet catastrophe”. **Yet how did Einstein intended to resolve the paradox?**

517 In the second part of his 1905a chef-d-euvre Einstein applies thermodynam-
518 ics, statistical mechanics and maxwellian electrodynamics to peer at the domain
519 of empirical reality covered by Wien’s radiation law. Einstein takes $\beta = h/k = Nh/R$
520 (R denotes the universal gas constant, N the number of “real molecules” in one
521 gram-equivalent, h is Planck’s constant and k is Boltzmann’s constant) as undefined
522 constant in 1905a paper and hence he writes $R\beta/N$ everywhere instead of h . The
523 joint application of the three mature theories enables Einstein to arrive at appar-
524 ently deductive argument: if monochromatic radiation of frequency ν and energy E
525 is enclosed in the volume V_0 , then the probability W that at any moment all the
526 radiation energy will be found in the partial volume V of the volume V_0 is given by
527

$$W = (V/V_0)^{E/h\nu} \quad (1)$$

528 Yet in the same paper Einstein had previously ascertained that in the case of n
529 independently moving particles enclosed in a volume V_0 the probability of finding
530 them all momentarily in the subvolume V is
531

$$W = (V/V_0)^n \quad (2)$$

532 Comparing Eqs. (1) and (2), Einstein draws a startling conclusion that “*mono-*
533 *chromatic radiation of small density behaves in thermodynamic respects as though*
534 *it consists of distinct independent energy quanta of magnitude $h\nu$ ”.*

535 Thus, the upshot that radiation in the cavity consists of independent energy
536 quanta follows *directly* from application of general principles of thermodynamics
537 and statistical mechanics to radiation phenomena.

538 But in 1905 all the available experimental data, relevant to fluorescence, pho-
539 toelectricity and photoionization data, provided only *indirect* evidence in favor of
540 quantum hypothesis. Hence, to carefully check the ultra-revolutionary hypothesis of

541 quanta, Einstein had to perform a “*crucial experiment*” of a very peculiar, freaky
542 kind. He had to compare the quantum results with the results of another entrenched,
543 ‘old’ theory contrived *independently* of the 1905a hypothesis. It is important that
544 this theory had to be sufficiently ‘old’ to accumulate the results of many experi-
545 ments. So, if the 1905a paper results had matched the results of fairly different the-
546 ory, that sprung out of substantially different problem situation, they would have
547 provided an especially reliable verification of “photon hypothesis”. Let us recall that

548 A proposition is correct if, within a logical system, it is deduced according to
549 the accepted logical rules. A system has truth-content according to the cer-
550 tainty and completeness of its coordination-possibility to the totality of expe-
551 rience. A correct proposition borrows its ‘truth’ from the truth-content of a
552 system to which it belongs [Ein richtiger Satz erborgt seine ‘Wahrheit’ von
553 dem Wahrheits-Gehalt des Systems, dem er angehört] (Einstein 1949a, p. 13).

554 In the opposite case the 1905a theory would have ‘falsified’ not by a single ‘criti-
555 cal experiment’ but by a whole multitude of the well-established experimental
556 data. What I want to stress is that it was this ‘holistic’ stand that allowed Einstein
557 as early as in 1906 to disregard the results of Kaufmann’s “crucial” experiments,
558 which seemed to corroborate the Abraham–Bucherer theory and to refute the “Lor-
559 entz–Einstein” theory (Holton 1968, p. 253; Miller 1981, p. 124).

560 As Einstein had put it, the rival theories (e.g. Abraham’s electron theory)

561 Have rather small probabilities, because their fundamental assumptions (con-
562 cerning the mass of moving electrons) are not explainable in terms of theo-
563 retical systems which embrace a greater complex of phenomena (Einstein as
564 quoted in Holton 1968, p. 253).

565 Thus the next—1905b—result turned out to be crucial for the 1905a verification. In
566 the 1905b paper Einstein assiduously worked out the principles of Brownian motion
567 that were directly verified by Perrin’s experiments.

568 My principal aim in this [1905b work on Brownian motion] was to find facts
569 that would guarantee as much as possible the existence of atoms of definite
570 size... The agreement of these considerations with experience together with
571 Planck’s determination of the true molecular size from the law of radiation (for
572 high temperatures) convinced the sceptics, who were quite numerous at that
573 time (Ostwald, *Mach*), of the *reality of atoms* (Einstein 1949a, pp. 45–47; my
574 italics).

575 Though the importance of 1905b paper’s for the 1905a one was promulgated by
576 Einstein much later; he confessed to Max von Laue on 17 January 1952:

577 When one goes through your collection of verifications of the special relativity
578 theory, one believes that Maxwell’s theory is firmly established. But in 1905 I
579 knew *already with certainty* that it leads to the wrong fluctuations in radiation
580 pressure, and consequently to an incorrect Brownian motion of a mirror in a
581 Planckian radiation cavity (quoted from Rynasiewicz 2000, p. 177; my italics).

582 This evident for 1905 Einstein result was posited to the scientific community only
583 in 1909 when Einstein applied his theory of Brownian motion to a two-sided mirror
584 immersed in thermal radiation. He demonstrated that the mirror would be unable to
585 carry out a Brownian motion indefinitely, if the fluctuations in the radiation pressure
586 on its surfaces were solely due to the effects of random waves, as predicted by Max-
587 well's theory. But only the presence of an additional term, corresponding to pres-
588 sure fluctuations due to the impact of random particles, guarantees the continued
589 Brownian motion of the mirror. Einstein exhibited that similar fluctuation terms in
590 the energy were consequences of Planck's law. He took such fluctuation phenomena
591 as the *strongest argument* for ascribing physical significance to the hypothetical light
592 quanta (Stachel 2000). Only after this queer "crucial experiment", that is only *after*
593 the 1905b paper could Einstein look forward for investigating the consequences of
594 his light quantum hypothesis, and so he returned to his half-forgotten "unsere Arbeit
595 uber die Relativbewegung", eine "kapitale Abhandlung". So far, so good.

596 If the monochromatic radiation (of sufficiently small density) in the sense of
597 entropy dependence upon volume behaves itself as a discontinuous medium,
598 consisting of energy quanta $R\beta\nu/N$, a question occurs: if they are not the laws
599 of creation and conversion of light such as if it consists of similar energy
600 quanta? (Einstein 1905a, p. 236).

601 That is the question put up by Einstein at the end of § 6 of his 1905a. But *the ether*
602 *conception turned out to be a considerable snag. It prevented positive answer and*
603 *put insurmountable obstacles in uncoiling Einstein's statistical-thermodynamics*
604 *programme. Indeed*

605 mechanical and purely electromagnetic interpretations of optical and electro-
606 magnetic phenomena have in common that in both cases electromagnetic field
607 is considered as a special state of the hypothetical medium filling all the space.
608 Namely in that point two interpretations mentioned differ radically from New-
609 ton's emission theory, in which light consists of moving particles. According
610 to Newton, space should be considered as possessing neither ponderable mat-
611 ter, nor light rays, i.e. absolutely empty (Einstein 1905a, p. 236).

612 To *contrive* a quantum theory of radiation, one needs electromagnetic fields as *inde-*
613 *pendent* entities that can be emitted by the source "just as in Newton's emitting
614 theory" (i.e. the energy transmitted in a process of emission should not be dissipated
615 in space, but should be *completely* preserved until an elementary act of absorption).
616 However, within the Lorentz programme an electromagnetic field is taken as a spe-
617 cific state of ether—a state of medium that is *continuously* distributed in space. In
618 such a medium an elementary process of radiation is connected only with a *spheri-*
619 *cal* wave.

620 Nevertheless, aversion to ether and acceptance of emission theory should lead
621 to Walter Ritz's 1908 'ballistic hypothesis': velocity of quantum should depend on
622 the velocity of its source. In Ritz's theory the velocity of light is not constant, but is
623 equal to $v+c$, where v is a relative velocity of the observer and the source.

624 Later, in April of 1922, Einstein had confessed to Viscardini:

625 I rejected this [emission] hypothesis at that time, because it leads to tremen-
626 dous theoretical difficulties (e.g. the expectation of shadow formation by a
627 screen that moves relative to the light source) (quoted from Rynasiewicz 2000,
628 p. 182).

629 Thus Einstein, by contrast, never thought of downing Maxwell's theory, just
630 as Newton, the inventor of the emission theory, did not reject the wave theory
631 300 years earlier. In the 1905a light-quanta paper Einstein had especially under-
632 scored that

633 Wave theory operating with point continuous functions is *excellently* justi-
634 fied when describing purely optical phenomena and perhaps would not be
635 replaced by another theory (Einstein 1905a, p. 237; my italics).

636 In Lorentz's theory this stumbling block was absent. Indeed, in the reference frame
637 that is at rest relative to the ether light propagates with constant velocity *independ-*
638 *ent of the velocity of the source*. Hence, if one intends to give up the idea of ether,
639 but to come to terms with Maxwell's theory at the same time, s/he should disown
640 ballistic hypothesis and "raise to the rank of a principle the validity of the law of
641 constancy of light velocity for all inertial frames" (Einstein 1936/1954, p. 307), i.e.
642 ***postulate a special "principle of constancy of velocity of light"(I).***

643 The second basic principle of STR—"the principle of relativity"(II)—follows
644 immediately from the tenet that there is no luminiferous ether and, consequently,
645 no absolute system of reference.

646 Just as Einstein colourfully recollected in the "Autobiographical Notes",

647 Reflections of *this type* [i.e. on molecular structure of radiation] made it
648 clear to me as long as shortly after 1900, i.e. shortly after Planck's trailblaz-
649 ing work, that neither mechanics nor electrodynamics could (except in lim-
650 iting cases) claim exact validity. By and by I despaired of the possibility of
651 discovering the true laws by means of constructive efforts based on known
652 facts. The longer and the more despairingly I tried, the more I came to the
653 conviction that only the discovery of a ***universal formal principle*** could
654 lead us to assured results. ***The example I saw before me was thermodynam-***
655 ***ics*** (Einstein 1949a, p. 51; my bold italics).

656 The latter point needs elucidation at the expense of delving into the basic source
657 of 1905 Einstein's information on the history of physics—to Mach's fascinating
658 "*Mechanics*".

659 The most profound case study of the interconnection between the principle
660 of economy of thought and second law of thermodynamics in Mach's "*Mechan-*
661 *ics*" is Stevinus's (1548–1620) theoretical scheme of statics. In the "*Hypomne-*
662 *mata Mathematica*" (Leyden 1605) Stevinus was one of the first to investigate
663 the mechanical properties of the inclined plane. His ultimate aim was to set up a
664 general theoretical principle and then to proceed to partial cases that can be easily
665 treated by quantitative means. To produce the pivotal gedankenexperiment, nec-
666 essary to set up his general principle, Stevin contrives a triangular prism with no
667 horizontally placed edges. Over the prism he lays an endless string on which 14

668 balls of equal weight are strung and tied at equal distances apart. (The string can
669 be advantageously replaced by an endless uniform chain).

670 Now, the chain will either be in equilibrium or not. If one assumes the lat-
671 ter to be the case, the chain, since the conditions of the event are not altered by
672 its motion, must, when once actually in motion, continue to move forever. In
673 other words, it must present perpetual motion, which Stevin takes apparently
674 absurd. Hence only the first case is conceivable and *the chain always remains in*
675 *equilibrium*.

676 It is crucial for Mach that in the basic premise from which Stevin starts, that *the*
677 *endless chain does not move*, there is contained only a *purely instinctive* cognition.
678 He feels at once, and we with him, that we have never observed anything like a
679 motion of the kind referred to. This conviction has so much logical cogency that
680 one accepts the conclusion drawn from it respecting the law of equilibrium on the
681 inclined plane without the thought of an objection, *although the law is slyly pre-*
682 *sented as the simple result of the experiment*. We cannot be surprised at this when
683 we reflect that all results of experiment are obscured by adventitious circumstances
684 (as friction, etc.), and that every conjecture as to the conditions which are determi-
685 native in a given case are liable to error. Thus Stevinus ascribes to instinctive knowl-
686 edge of this sort a *higher authority* than to simple, manifest, direct observations!

687 As a result, the following question forces itself upon us: *whence does this higher*
688 *authority come?* If one recalls that scientific demonstration, and scientific criticism
689 generally can only have sprung from the consciousness of the individual fallibility
690 of investigators, the explanation is not far to seek. We feel clearly, that we ourselves
691 have contributed *nothing* to the creation of this “*Instinctive Knowledge*”, that we
692 have added to it nothing arbitrarily, but that it exists in absolute independence of our
693 participation.

694 According to “*Mechanics*”, Stevinus’s deduction is one of the rarest ‘fossile indi-
695 cators’ that we possess in the primitive history of mechanics, and throws a won-
696 derful light on the process of the formation of science generally, on its rise from
697 instinctive knowledge. Nevertheless, every experimenter can daily observe in his
698 own person the guidance that Instinctive Knowledge furnishes him. If he succeeds in
699 *abstractly formulating* what is contained in it, he will as a rule have made an impor-
700 tant advance in science, And it is perfectly certain for Mach that the union of the
701 strongest instinct with the greatest power of abstract formulation alone constitutes
702 the great natural inquirer [Mach 1893/1999: p. 27].

703 But how does this “instinctive knowledge” originate and what are its contents?

704 Everything which we observe in nature imprints itself *uncomprehended* and
705 *unanalysed* in our percepts and ideas. In these accumulated experiences we possess
706 a ‘treasure store’ which is ever close at hand and of which only the smallest portion
707 is embodied in fine articulate thought. The circumstance that it is far easier to resort
708 to these experiences than it is to nature herself, and they are, notwithstanding this,
709 free, in the sense indicated, from all subjectivity, *invests them with a high value*. “*It*
710 *is a peculiar property of instinctive knowledge that it is predominantly of a negative*
711 *nature*” [Mach 1893/1999: p. 28]. We cannot so well say what must happen as we
712 can what cannot happen, since the latter alone stands in devastating contrast to the
713 obscure mass of experience in us in which single characters are not distinguished.

714 Moreover, contends Mach, the other peculiar trait that is extremely important for the
715 philosophy of science consists in that the reasoning of Stevinus has such a strong
716 influence upon us because the result at which he arrives apparently contains *more*
717 than the assumption from which he starts.

718 Furthermore, it often happens in the course of the advancement of science that
719 a new principle perceived by some researcher in connection with a fact, is not
720 immediately recognized and rendered familiar in all its generosity. If, throughout
721 all facts, we clearly *see* and *discern* a principle which, though not admitting of
722 proof, can yet be known to *prevail*, we have advanced much farther in the consist-
723 ent conception of nature than if we suffered ourselves to be overawed by a spe-
724 cious demonstration.

725 Eventually,

726 It is more in keeping, furthermore, with the *economy of thought* and with
727 the aesthetics of science, directly to *recognise* a principle (say that of the
728 statical moments) as the key to the understanding of *all* the facts of a depart-
729 ment, and *really* see how it *pervades* all those facts, rather to hold ourselves
730 obliged first to make a clumsy and lame deduction of it from unoblivious
731 propositions that involve the same principle but that happen to have become
732 earlier familiar to us [Mach 1893/1999, p. 82].

733 On my view, *all the abovementioned Stevin–Mach recipes where ingeniously*
734 *implemented by Einstein in formulating the basic STR principle—the principle*
735 *of relativity*. Though due to ultra-revolutionary and extremely speculative nature
736 of light-quanta hypothesis he could not afford himself to reveal the link with the
737 1905a paper directly. Hence he applied all the Stevin–Mach technique of convic-
738 tion to *posit his electrodynamics of moving bodies in phenomenological wake*.
739 One should especially take into account the *negative character of the relativity*
740 *principle* and the manner of its connections with experiments and observations
741 that is closer to instinctive knowledge subtle conviction technique than to coarse
742 inductive way of inference. Look at the beginning of the STR paper:

743 Examples of a similar kind, and the failure of attempts to detect a motion
744 of the earth relative to the ‘light medium’, lead to the *conjecture* that not
745 only in mechanics, but in electrodynamics as well, the phenomena *do not*
746 have any properties corresponding to the concept of absolute rest, but that
747 in all coordinate systems in which the mechanical equations are valid, also
748 the same electrodynamic and optical laws are valid, as have already been
749 shown for quantities of the first order. We shall raise this conjecture (whose
750 content will be called ‘the principle of relativity’ hereafter) to the status of
751 a postulate and shall introduce, in addition, the postulate, only seemingly
752 incompatible with the former one, that in empty space light is always propa-
753 gated with a definite velocity V which is independent of the state of motion
754 of emitting body (Einstein 1905d, p. 140; my italics).

755 Appeal to *instinctive knowledge* easily explains the fact that the special relativ-
756 ity paper stands out in all the world scientific literature for the **complete lack of**
757 **quotations**.

758 And since, according to the “*Autobiographical Notes*”, Einstein’s new theory
759 was created as a result of inevitable encounter of Newtonian mechanics and Max-
760 wellian electrodynamics, its basis should consist of a *minimum* of two postulates,
761 (I) the first drawn from classical mechanics (the principle of relativity) and (II)
762 the second one transferred from the Maxwell–Lorentz electrodynamics (the prin-
763 ciple of the constancy of light). Namely,

764 (I) *Classical mechanics*, of which it could not be doubted that it holds with
765 a close degree of approximation, teaches the equivalence of all inertial sys-
766 tems or inertial ‘spaces’ for the formulation of natural laws, i.e., the invari-
767 ance of natural laws with respect to the transition from one inertial system
768 to another (Einstein 1954, p. 369).

769 (II) This [the special theory of relativity] takes over from the *theory of*
770 *Maxwell–Lorentz* the assumption of the constancy of the velocity of light
771 (Einstein 1940/1954, p. 370).

772 The two postulates, (I) + (II), the relativity principle plus the principle of con-
773 stancy of velocity of light, are quite sufficient, according to Einstein, to contrive
774 the electrodynamics of moving bodies. Yet, since “the theory based on these two
775 principles should not to lead to contradictory results, one must renounce the cus-
776 tomary rule of addition of velocities “ (Einstein 1910, p. 125).

777 And namely that was done in the 1905d paper «*On the Electrodynamics of*
778 *Moving Bodies*”, published several months *after* the photon paper. Einstein had
779 dug out the hidden assumption—the basis of the Galileo addition law—that the
780 statements of time, as well as of the shapes of moving bodies have the sense inde-
781 pendent of the state of motion of the reference frame. He revealed that the accept-
782 ance of the “principle of relativity” together with the “principle of constancy of
783 light” is equivalent to modification of the simultaneity concept and to clock delay
784 in moving reference frame.

785 It should be stressed that in no ways 1905 Einstein was an idle thinker contem-
786 plating on the essence of space and time. He was *forced* to elevated philosophical
787 reflections on the nature of space and time by his *research practice*, by a mun-
788 dane physical problem of reconciling classical mechanics (the Principle of Relat-
789 ivity) with classical electrodynamics (the Light Constancy Postulate).

790 Hence, at least in that case, Einstein’s use of Hume and Mach’s philosophical
791 writings was “*highly selective*” (Norton 2010, p. 359). His ultimate goals were
792 not so much to apprehend Hume’s and Mach’s refined philosophical reflections
793 as to find in them concrete ideas that may be useful in his mundane research
794 practice.

795 Well, if all the aforesaid is true, the abovementioned question should be scruti-
796 nized: *why Einstein in the 1905d relativity paper did not cite his 1905a paper on*
797 *light quanta?*

798 To give a judicious answer one has to dwell into Einstein’s 1905 correspondence.
799 Writing to his close friend Conrad Habicht in 1905 and sending him the fruits of

800 his labours at that time, Einstein called his light quanta paper “*very revolutionary*”,
801 while the relativity paper was humbly characterized as “*interesting* in its kinemati-
802 cal part”. So, *reference in the paper, making significant changes mainly of metaphys-*
803 *ical character, on the hypothesis that had already introduced revolutionary changes*
804 *and had obviously contradicted Maxwell’s theory, could hardly make the arguments*
805 *stronger.*

806 Einstein himself at the first Solvay Congress had to admit “provisional char-
807 acter of this concept [light quanta] which does not seem reconcilable with the
808 experimentally verified consequences of the wave theory” (quoted from Pais
809 1979, p. 884). The situation was even worse since *direct experimental evidence*
810 *in favour of existence of light quanta was absent. It famously appeared only circa*
811 *1923 (the Compton effect).*

812 Being taken independently, the STR did not explain any *new* experimental
813 fact. Predictions of the Lorentz theory were identical to that of the STR, so that
814 it would not be possible in any case to distinguish between the two theories on
815 experimental grounds. Moreover, most of Einstein’s contemporaries had scruti-
816 nized the “Lorentz–Einstein electron model”, reflected on the “principle of rela-
817 tivity of Lorentz and Einstein”, and so forth. At the time of publication of Lor-
818 entz’s second order theory (1904) the only data available to test these theories
819 were Kaufmann’s notorious measurements of the masses of slowly moving elec-
820 trons. But they were initially interpreted as contradicting *both* STR and Lorentz’s
821 theory. It took a year for Einstein to answer on Kaufmann’s paper. One can imag-
822 ine how the STR was evaluated by the scientific community in 1905–1906!

823 Furthermore, cautious Einstein did not promulgate the connections between
824 1905a and 1905d until 1909. However, *without this links the STR postulates can*
825 *be evaluated as ad hoc hypotheses. And they were!* (The reaction of Henri Poin-
826 caré and of the French school is the most blatant example). So, being confronted
827 with many rival theories, why did Einstein preferred special theory of relativity?
828 What undisguised advantages did it have over the artful theories of Lorentz, Ritz
829 and others?

830 The answer leads one to Einstein’s unificationist approach once more. The uni-
831 ficationist stand illuminates Einstein’s seemingly puzzling remarks that despite
832 the underdetermination at any given time there **is** only one correct theory: the
833 theory with the *greatest power of unification* at that time (Einstein 1918; see Bel-
834 ler 2000 for details).

835 We are usually told that in constructing special relativity Einstein had invented
836 a “*theory of principle*”, rather than a “*constructive theory*”. Yet things are not
837 that simple.

838 Indeed, it was Einstein himself who ascertained a thought-provoking distinc-
839 tion between ‘principle’ theories and ‘constructive’ ones. Constructive theories
840 try to “build up a picture of the more complex phenomena out of the materials
841 of a relatively simple formal scheme from which they start out” (Einstein 1919
842 as quoted from van Dongen 2010, p. 49). An example of a constructive theory
843 is kinetic theory that attempts at reducing mechanical and thermal properties of
844 gases to movements of molecules, as well as Einstein’s light quanta hypothesis
845 for the same reasons.

846 On the contrary, principle theories do not start out from hypothetical construc-
847 tions, but rather from empirically ascertained principles.

848 Thus the science of thermodynamics seeks by analytical means to deduce
849 necessary conditions, which separate events have to satisfy, from the uni-
850 versally experienced fact that perpetual motion is impossible'. In explicitly
851 Kantian terms Einstein in 1919 distinguishes between the abovementioned
852 kinds of theories: "principal theories employ the *analytic*, not the *synthetic*
853 method (quoted from van Dongen 2010, p. 50).

854 Prima facie it is to his boon companion Michele Besso that Einstein dedicated the
855 only acknowledgement in his 1905d paper, the paper that stands out for its *lack*
856 *of any reference to the literature*. Furthermore, in the 1905d paper "the failure of
857 attempts to detect a motion of the earth relative to the 'light medium'" is used
858 as evidential support only for *one* of the two basic postulates—for the "Principle
859 of Relativity". The "Light Postulate" is introduced almost parenthetically, with-
860 out any discussion of its experimental grounds. Only in the 1905e paper, while
861 describing the 1905d paper results, Einstein drops a telling phrase: "the principle
862 of the constancy of the velocity of light used there is of course contained in Max-
863 well's equations" (Einstein 1989, 172). Yet do not forget that for him the 1905d
864 paper was only a provisional construct, only a milestone in realizing the unifica-
865 tion programme. Einstein himself realized that

866 a physical theory can only be satisfactory, if its structures are composed of
867 elementary foundations. The theory of relativity is just as little ultimately
868 satisfactory as, for example, classical thermodynamics was before Boltz-
869 mann had interpreted the entropy as probability (Einstein to Arnold Som-
870 merfeld on 14 January 1909; quoted from Stachel 2000, p. 10)].

871 So, the statement that 1905d paper constituted a theory of principle is merely
872 *half of the truth*. In reality the 1905d theory was a constructive one that only
873 *posited itself* as a theory of principle (possibly due to tactical reasons for Einstein
874 probably tried to save the STR from the scathing criticism directed against the
875 light quanta). That is why two years later, trying to elicit the STR foundations to
876 broad physical community, Einstein humbly described his relativity theory as "an
877 attempt to summarize the studies that have resulted to date from the *merger* of the
878 H.A. Lorentz's theory and the principle of relativity" (Einstein 1907, p. 253).

879 But the situation could not last over a long period of time. Einstein had to
880 throw his cards up and to unfold the link between his 1905a and 1905d papers
881 4 years later. In 1909, in Salzburg, he made a report at the 81-st meeting of Ger-
882 man Natural Scientists and Physicians under the self-explanatory heading "*On*
883 *the Development of our Views on the Nature and Structure of Radiation*". It
884 represented practically the first effort to comprehend all his various papers as a
885 whole. And it was one of the first public reports of the STR inventor dedicated to
886 expounding of its foundations. The report starts with a succinct recapitulation of
887 luminiferous ether theory that ends by an intriguing question: "However, today
888 we must regard the ether hypothesis as an obsolete standpoint".

889 **Why?** - What I want to stress is that *for the answer Einstein dwells not to the*
890 *Michelson–Morley* or Fizeau experiments, but elucidates that

891 It is even undeniable that there is an extensive group of facts concerning
892 radiation that shows that light possesses certain fundamental properties that
893 can be understood far more readily from the standpoint of Newton's *emis-*
894 *sion theory of light* than from the standpoint of the wave theory. It is there-
895 fore my opinion that the next stage in the development of theoretical physics
896 will bring us a theory of light that can be understood as a kind of *fusion* of
897 the wave and emission theories of light (Einstein 1909, p. 379; my bold ital-
898 ics).

899 And the abovementioned experiments are brought into consideration only in the
900 context of the “cardinal aspect in which the electromagnetic theory agrees with, or,
901 more accurately, *seems to agree* with the kinetic theory” (Einstein 1909, p. 379; my
902 bold italics).

903 **4 Conclusions**

904 The basic claim to put forward is that to conceive the important facets of Einstein's
905 1905 scientific creativity and all his 1905 papers *as a whole* as well as the sub-
906 tle *order* of their presentation one should resort to Einstein's strenuous efforts to
907 reconcile maxwellian electrodynamics and statistical thermodynamics. In creating
908 the theory of light quanta and the special theory of relativity Einstein was operat-
909 ing according to a strong belief in the necessity for unity in science, as well as the
910 coincidence of both constructing theory and integrating intuition of Principle. He
911 is perhaps best known for the later, but in fact his ideas were built equally on the
912 former. Hence identifying and resolving the paradox revealing the contradictions
913 between the basic research traditions turns out a key part of the scientific method.
914 It was exhibited that Einstein's method was construction of theory within the guid-
915 ance of intuitive principles sometimes beginning with construction, sometimes with
916 principle, but always demanding their consistency, and clear identification of well-
917 documented paradox that forces us to consider a larger view of Nature's laws.

918 And to comprehend the importance of the latter one should turn to Mach's prin-
919 ciple of the economy of thought that was implemented by Einstein through and
920 through during all his life. Nevertheless, this is not to assert that 1905 Einstein was a
921 committed Machian incapable to draw upon the other epistemological sources.

922 Nope. For instance, in mature, profound and thoughtful “*Physik und Realität*”,
923 published in “*The Journal of the Franklin Institute*” in March 1936, Einstein
924 reconsidered the history of mechanics in *sharply* different from the author of “*Die*
925 *Mechanik*” way:

926 These two modes of application of mechanics [i.e. analytical mechan-
927 ics and the mechanics of continuous media] belong to the so-called “phe-
928 nomenological physics”. It is characteristic of this kind of physics that it
929 makes as much use as possible of concepts which are close to experience

930 but, for this reason, has to give up, to a large extent, *unity in the founda-*
931 *tions*. Heat, electricity, and light are described by separate variables of state
932 and material constants other than mechanical quantities, and to determine
933 all of these variables in their mutual and temporal dependence was a task
934 which, in the main, could only be solved empirically. Many contemporaries
935 of Maxwell saw in such a manner of presentation the ultimate aim of
936 physics, which they thought could be obtained purely inductively from experi-
937 ence on account of the relative closeness of the concepts used to experience.
938 From the point of view of theories of knowledge St. Mill and *E. Mach* took
939 their stand approximately on this ground. In my view, the greatest achieve-
940 ment of Newton's mechanics lies in the fact that its constant application has
941 *led beyond the phenomenological point of view*, particularly in the field of
942 heat phenomena. This occurred in the kinetic theory of gases and *in statisti-*
943 *cal mechanics in general*. The former connected the equation of state of
944 the ideal gases, viscosity, diffusion, and heat conductivity of gases and radio-
945 metric phenomena of gases, and gave the *logical connection* of phenomena,
946 which from the point of view of direct experience, had nothing whatever to
947 do with one another (Einstein 1936/1954, 302; my italics).

948 Thus, inevitable divergences of opinion with Mach sprung out not only from
949 stubborn development of atomic theory by Einstein through his 1905 scrutinizing
950 of Brownian motion (Einstein 1905b). They also consisted in advancing the simi-
951 lar idea of 'atoms of light' (Einstein 1905a). In my view, to comprehend the more
952 profound reasons of the abovementioned divergences one has to turn face to face
953 to Einstein's true overall philosophical standpoint.

954 All in all, this standpoint can be characterized as '*eclecticism*', and one can-
955 not elude quoting the famous passage from Einstein's 1949 "*Reply to Criticism*"
956 where he acknowledges that

957 The scientist, however, cannot afford to carry his striving for epistemologi-
958 cal systematic that far. He accepts gratefully the epistemological conceptual
959 analysis; but the *external conditions*, which are set for him by the facts of
960 experience, do not permit him to let himself be too much restricted in the
961 *construction of his conceptual world* by the adherence to an epistemologi-
962 cal system. He therefore must appear to the systematic epistemologist as a
963 type of unscrupulous *opportunist*: he appears as *realist* insofar as he seeks
964 to describe a world independent of the acts of perception; as *idealist* inso-
965 far as he looks upon the concepts and theories as the free inventions of the
966 human spirit (not logically derivable from what is empirically given); as
967 *positivist* insofar as he considers his concepts and theories justified only to
968 the extent to which they furnish a logical representation of relations among
969 sensory experiences. He may even appear as *Platonist* or *Pythagorean* inso-
970 far as he considers the viewpoint of logical simplicity as an indispensable
971 and effective tool of his research (Einstein 1949b, 684; my italics).

972 More thoroughly, Einstein's own philosophy of science can be characterized
973 as a *quaint fusion* of the elements drawn from sources as diverse as "Machian
974 empiricism, Duhemian conventionalism and neo-Kantianism" (Howard 1994).

975 Lo and behold! The 1905a light quanta hypothesis is a *constructive* model of
976 radiation; so in the 1949 *Autobiographical Notes* Einstein recalled of Mach's legacy:

977 He [Mach] did not place in the correct light the *essentially constructive* and
978 speculative nature of all thinking and more especially of scientific thinking;
979 in consequence, he condemned theory precisely at those points where its
980 *constructive-speculative* character comes to light unmistakably, such as in
981 the kinetic theory of atoms (Einstein 1949a, p. 13).

982 Hence the constructive character of light quanta hypothesis inevitably brings
983 Einstein's thought closer to Kantian epistemology as was already pointed out by
984 many Einstein scholars.

985 For instance, in Victor F. Lenzen's exquisite essay "*Einstein's Theory of*
986 *Knowledge*" which Einstein himself hailed as "convincing and correct in every-
987 thing it says", it is maintained that

988 In so far as he acknowledges mathematical objects to be constructions, the
989 theory of Einstein reminds one of Kant who held that objects of mathemat-
990 ics were *constructed in pure intuition* (Lenzen 1949, p. 380; my italics).

991 In his bona fide 1949 account of Einstein's epistemology Victor F. Lenzen
992 stressed that during the second half of the XIXth century many scientists—but
993 Ernst Mach particularly—regarded the ultimate goal of physical science as the
994 representation of processes through concepts *inductively* derived from sense
995 experiences. Yet on Einstein's fledged view the consistent application of Newto-
996 nian mechanics carried theoretical physics far *beyond* the pure phenomenological
997 standpoint.

998 Likewise, according to the other earnest epistemologist from the abovementioned
999 Schilpp volume

1000 Einstein himself occupies an intermediate position between Cassirer's neo-
1001 Kantianism and Mach's positivism (Ushenko 1949, p. 609; see also Northrop
1002 1949, p. 390).

1003 It is a platitude that Einstein stubbornly and constantly emphasized that the basic
1004 concepts of science are *free creations* of the human mind. In that respect Einstein's
1005 views were evidently close to Kant. And the positive drive for creative work could
1006 be found in Kant's *constructivist* foundation for scientific knowledge that restricted
1007 science to the realm of appearances stating that a priori knowledge of things in
1008 themselves is impossible. Much later Einstein had admitted:

1009 I did not grow up in the Kantian tradition, but *came to understand* the truly
1010 valuable which is to be found in his doctrine, alongside of errors which today
1011 are quite obvious, quite late. It is contained in the sentence: 'The real is not
1012 given [gegeben] to us, but put to us [aufgegeben]' [by way of a riddle] (Ein-
1013 stein 1949, p. 680; quoted from Ryckman 2005).

1014 Even mathematics—maintained to be most stable and certain because of its
1015 being analytical—was comprehended by Kant as an a priori *synthetic judgement*.
1016 As he stressed in “*Prolegomena*” (Kant 1783/2002), the essential feature of pure
1017 mathematical cognition, differentiating it from all other a priori cognition, is that
1018 it must throughout proceed not from concepts, but always and only through the
1019 **construction** of concepts. Because pure mathematical cognition, in its proposi-
1020 tions, must therefore go beyond the concept to that which is contained in the *intu-*
1021 *ition* corresponding to it, its propositions can and must never arise through the
1022 analysis of concepts, i.e. analytically, and so are one and all synthetic.

1023 Correspondingly, in the passage of the “*Autobiographical Notes*’ relating to
1024 his childhood Einstein pointed out that “our thinking goes on for the most part
1025 without use of signs (words) and beyond that to a considerable degrees uncon-
1026 sciously” (Einstein 1949a, p. 9).

1027 Hence for him, beginning from his early years

1028 the objects with which geometry deals seemed to be of no different type
1029 than the objects of sensory perception, ‘which can be seen and touched’.
1030 This primitive idea, which probably also lies at the bottom of the well-
1031 known Kantian problematic concerning the possibility of ‘synthetic judge-
1032 ment a priori’ (Einstein 1949a, p. 11).

1033 The Kantian tenet of the intuitive character of mathematics means the limiting of
1034 mathematics to those objects that are constitutable [Konstruierbar]. ‘Intuitive’ is
1035 equal to ‘constitutable’. As Ludwig Wittgenstein has later coined it in genuinely
1036 Kantian fashion, “But the mathematician is not a discoverer, he is an *inventor*».

1037 Kant contemplated objectivity of science as resulting from the manner in
1038 which the manifold of sensibility was ordered under the categories of the under-
1039 standing by means of spatial and temporal categories. This is why mathematics
1040 could so effectively describe objective reality for Kant: mathematical constructs
1041 are related to the pure intuitions of space and time. (And this is why natural sci-
1042 ence must be mathematical).

1043 Hence mathematical statements are true in virtue of their application in experi-
1044 ence to exhibit the behavior of empirical bodies. While mathematical judgements
1045 are obtained through construction in pure intuition, they count as cognitions only
1046 because they are necessarily connected to experience in the sense that geometrical
1047 space was contemplated as a condition of appearance (Kant 1787/1998, p. 196;
1048 my italics).

1049 In a sense the abstract objects of a theory are constituted by the laws of the
1050 theory. And objectivity is connected not to the existence of things but to the
1051 *objective validity of relations*. Accordingly, in the 1905a paper, constructing the
1052 mathematical abstract object “light quanta” out of the basic objects of maxwellian
1053 electrodynamics and statistical thermodynamics, Einstein was bothered not with
1054 grasping the ‘essences’ of radiation phenomena. He grappled with the problems
1055 of **reconciling** the interrelations of different classical physics research traditions,
1056 i.e. maxwellian electrodynamics, statistical mechanics and thermodynamics. Let
1057 us recall that in their Proposal for Einstein’s Membership in the Prussian Acad-
1058 emy of Science, M. Planck et al. had famously emphasized that

1059 Einstein has a special talent for getting to the bottom of other scientists'
1060 newly emerging views and assertions, and for assessing *their relationship*
1061 *to each other* and to experience with surprising certainty (Doc. № 445 of
1062 Einstein 1987, p. 338; my italics).

1063 It is well-known that Einstein's philosophical evolution after the General Relativity,
1064 i.e. after 1915 carried him further and further from Humean and Machian unim-
1065 pressed empiricist bias toward profound Neo-Cantian tradition represented by Weyl,
1066 Eddington, Cassirer, Husserl et al. and the mathematical speculative methodology
1067 embodied in a sequence of unified theories. Thus I am not contending here that Ein-
1068 stein of 1905 was a thorough (neo) Kantian, trying to implement the murky and
1069 abstract tenets of "Critique" into his mundane research practice. Yet, in my hum-
1070 ble opinion, *the Kantian facet (which needs to be trialed by future research), of the*
1071 *seeds of Einstein's late methodology lie in his 1905 activity connected with his fruit-*
1072 *ful efforts to reconcile maxwellian electrodynamics and statistical thermodynamics.*

1073 To recapitulate, Einstein was undoubtedly influenced by Hume, Mach, Poin-
1074 caré, et al., and this is evinced in innumerable documents that embrace letters, lec-
1075 tures, oral communications, etc. relating to different periods of his life. However,
1076 if one dwells into his scientific papers, trying to elucidate Einstein's *modus oper-*
1077 *andi*, one finds out sober reasons to believe that *actually*, at least in 1905, in his
1078 **actual** research practice, he had held an epistemological position that can be labeled
1079 as a quaint blend of Machian and Kantian epistemologies. And the most important
1080 Machian concept necessary to comprehend Einstein's 1905 activity as a whole is
1081 Mach's principle of economy of thought taken in the context of intuitive knowledge
1082 principle. Hence the ether notion was relinquished not because it was a metaphys-
1083 ical, idle concept, an obsolete superfluous contraption, but since it turned out a snag
1084 for reconciliation of maxwellian electrodynamics and statistical thermodynamics
1085 that promised to pave the way to theory of quanta. In theory choice situation one
1086 chooses the theory that is more fruitful in empirical respect and parsimonious in
1087 principle.

1088 In a nutshell, Einstein's '**scientific method**' turns out to embrace the following
1089 necessary steps.

- 1090 (1) Eduction of the **paradox** that cannot be circumvented by common expedients
1091 and evasions (the "ultraviolet catastrophe"). The startling paradox evinces the
1092 contradictions between the basic 'old' research traditions (maxwellian electro-
1093 dynamics, classical mechanics and thermodynamics). The revelation of the
1094 paradox presupposes that the ultimate means of its resolution should consist in
1095 reconciliation of the 'old' research traditions in the 'new' synthesis.
- 1096 (2) Awareness of the fact that the immediate resolution of the paradox is impossible
1097 since the necessary transformations of the 'old' research traditions are too radi-
1098 cal.
- 1099 (3) Nevertheless, the ultimate way of the resolution of the paradox is comprehended
1100 and the upper floors (light quanta hypothesis) of the future fusion theory are suc-
1101 cessfully constructed with the guidance of the corresponding intuitive principles
1102 (Kant). A subtle plan of unification that outlines how the changes should be

- 1103 performed from the upper floors to the lower ones, embracing a row of stages,
1104 is surmised.
- 1105 (4) One of the intermediate stages of fusion—the enunciation, keeping with the
1106 economy of thought and with a help of Stevinus–Mach instinctive-knowledge
1107 technique, of the **Universal Formal Principle** that indicates the ways of trans-
1108 forming the ‘old’ theories. It is a peculiar property of instinctive knowledge that
1109 the Universal Formal Principle (the principle of relativity) is predominantly of
1110 a negative character.
- 1111 (5) A thorough **recheck** of all the existing knowledge is carried out in order to elimi-
1112 nate the possible contradictions—either internal ones (the STR creation)—or the
1113 contradictions with other mature theories (the development of theory of energy
1114 and pressure fluctuations).

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