Halting problem proofs refuted on the basis of software engineering

This is an explanation of a key new insight into the halting problem provided in the language of software engineering. Technical computer science terms are explained using software engineering terms. No knowledge of the halting problem is required.

It is based on fully operational software executed in the x86utm operating system. The x86utm operating system (based on an excellent open source x86 emulator) was created to study the details of the halting problem proof counter-examples at the much higher level of abstraction of C/x86.

To fully understand this paper a software engineer must be an expert in:

- (a) The C programming language.
- (b) The x86 programming language.
- (c) Exactly how C translates into x86 (how C function calls are implemented in x86).
- (d) The ability to recognize infinite recursion at the x86 assembly language level.

The computer science term "halting" means that a Turing Machine terminated normally reaching its last instruction known as its "final state". This is the same idea as when a function returns to its caller as opposed to and contrast with getting stuck in an infinite loop or infinite recursion.

In computability theory, the halting problem is the problem of determining, from a description of an arbitrary computer program and an input, whether the program will finish running, or continue to run forever. Alan Turing proved in 1936 that a general algorithm to solve the halting problem for all possible program-input pairs cannot exist.

For any program H that might determine if programs halt, a "pathological" program P, called with some input, can pass its own source and its input to H and then specifically do the opposite of what H predicts P will do. No H can exist that handles this case. https://en.wikipedia.org/wiki/Halting_problem

The computer science term "halting" means that a Turing Machine terminated normally reaching its last instruction known as its "final state". This is the same idea as when a function returns to its caller as opposed to and contrast with getting stuck in an infinite loop or infinite recursion.

This general principle refutes conventional halting problem proofs

Every simulating halt decider that correctly simulates its input until it correctly determines that this simulated input would never reach its final state, correctly rejects this input as non-halting.

From a purely software engineering perspective H(P,P) is required to correctly predict that its correct and complete x86 emulation of its input would never reach the "ret" instruction of this input and H must do this in a finite number of steps.

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H0 correctly determines that Infinite_Loop() never halts

```
void Infinite_Loop()
    HERE: goto HERE;
int main()
    Output("Input_Halts = ", HO((u32)Infinite_Loop));
_Infinite_Loop()
[00001102](01) 55
[00001103](02) 8bec
[00001105](02) ebfe
[00001107](01) 5d
[00001108](01) c3
                                                             push ebp
                                                             mov ebp,esp
jmp 00001105
                                   8bec
                                    ebfe
                                                             pop ebp
 Size in bytes: (0007) [00001108]
_main()
[00001192](01)
[00001193](02)
[00001195](05)
[0000119a](05)
[0000119f](03)
[000011a2](01)
                                                             push ebp
                                    8bec mov ebp,esp
6802110000 push 00001102
e8d3fbffff call 00000d72
                                    83c404
                                                             add esp,+04
                                    50 push eax
68a3040000 push 000004a3
e845f3ffff call 000004f2
[000011a2](01) 50 push
[000011a3](05) 68a3040000 push
[000011ad](05) e845f3ffff call
[000011ad](03) 83c408 add (
[000011b0](02) 33c0 xor (
[000011b2](01) 5d pop (
[000011b3](01) c3 ret
Size in bytes:(0034) [000011b3]
                                                            add esp,+08
xor eax,eax
pop ebp
  machine
                        stack
                                                stack
                                                                      machine
                                                                                               assembly
                         address
                                                                      code
   address
                                                data
                                                                                                language
 [00001192] [00101ef8] [00000000] [00001193] [00101ef8] [00000000] [00001195] [00101ef4] [00001102] [0000119a] [00101ef0] [0000119f]
                                                                                               push ebp
                                                                     8bec mov ebp,esp
6802110000 push 00001102
e8d3fbffff call 00000d72
HO: Begin Simulation Execution Trace Stored at:211fac [00001102][00211f9c][00211fa0] 55 push ebp [00001103][00211f9c][00211fa0] 8bec mov ebp,esp [00001105][00211f9c][00211fa0] ebfe jmp 00001105 [00001105][00211fa0] ebfe jmp 00001105
HO: Infinite Loop Detected Simulation Stopped
  return 1;
 [0000119f][00101ef8][00000000] 83c404 add esp,+04 [000011a2][00101ef4][00000000] 50 push eax [000011a3][00101ef0][000004a3] 68a3040000 push 000004a3 [000011a8][00101ef0][000004a3] e845f3ffff call 000004f2
Input_Halts = 0
[000011ad][00101ef8][0000000] 83c408
[000011b0][00101ef8][00000000] 33c0
[000011b2][00101efc][00100000] 5d
[000011b3][00101f00][00000004] c3
                                                                                               add esp,+08
                                                                                               xor eax eax
                                                                                               pop ebp
                                                                                               ret
Number of Instructions Executed(554) == 8 Pages
```

H correctly determines that Infinite_Recursion() never halts

```
void Infinite_Recursion(int N)
     Infinite_Recursion(N);
 int main()
     Output("Input_Halts = ", H((u32)Infinite_Recursion, 0x777));
_Infinite_Recursion()
[000010f2](01) 55
[000010f3](02) 8bec
[000010f5](03) 8b4500
[000010f8](01) 50
[000010f9](05) e8f4f-
[000010fe](03) 83c400
[00001101](01) 5d
[00001102](01) c3
Size in bytes:(0017)
                                                           push ebp
                                                          mov ebp,esp
mov eax,[ebp+08]
                                   8b4508
                                                           push eax
                                   e8f4ffffff call 000010f2
                                  83c404
                                                           add esp,+04
                                                          pop ebp
 Size in bytes: (0017) [00001102]
_main()
[000011b2](01)
[000011b3](02)
[000011b3](05)
[000011b4](05)
[000011c4](03)
[000011c7](01)
[000011c4](05)
[000011c4](05)
[000011d2](03)
[000011d7](01)
[000011d8](01)
Size in bytes:
                                                           push ebp
                                  8bec mov ebp,esp
6877070000 push 00000777
68f2100000 push 000010f2
e8aefdffff call 00000f72
                                   83c408
                                                           add esp,+08
                                  50 push eax
68a3040000 push 000004a3
e820f3ffff call 000004f2
                                                          add esp,+08
xor eax,eax
pop ebp
                                  83c408
                                   33c0
                                   5d
 Size in bytes:(0039) [000011d8]
                                                                   machine
   machine
                        stack
                                              stack
                                                                                           assembly
                                                                                           language
   address
                        address
                                              data
                                                                   code
 [000011b2] [00101f39] [00000000] [000011b3] [00101f39] [00000000] [000011b5] [00101f35] [0000777] [000011ba] [00101f31] [000010f2] [000011bf] [00101f2d] [000011c4]
                                                                   55
                                                                                           push ebp
                                                                  8bec mov ebp,esp
6877070000 push 00000777
68f2100000 push 000010f2
e8aefdffff call 00000f72
mov ebp,esp
mov eax,[ebp+08]
                                                                   50 push eax // push 0x777
e8f4ffffff call 000010f2 // call Infinite_Recursion
                                                                  8b4508 mov eax,[ebp+08]
50 push eax // push 0x777
e8f4ffffff call 000010f2 // call Infinite_Recursion
 H: Infinite Recursion Detected Simulation Stopped
  if (current->Simplified_Opcode == CALL)
if (current->Simplified_Opcode == traced->Simplified_Opcode) // CALL
if (current->Address == traced->Address) // from
if (current->Decode_Target == traced->Decode_Target) // to So
if (Conditional_Branch_Count == 0) // no exercise.
                                                                                                                                              from same address
                                                                                                                                         // to Same Function
                                                                                                                                         // no escape
[000011c4] [00101f39] [00000000] 83c408 [000011c7] [00101f35] [00000000] 50 [000011c8] [00101f31] [000004a3] 68a3040 [000011cd] [00101f31] [000004a3] e820f3f1 [000011d2] [00101f39] [00000000] 83c408 [000011d5] [00101f39] [00000001] 33c0 [000011d7] [00101f3d] [0000018] 5d [000011d8] [00101f41] [00000000] c3
                                                                                           add esp,+08
                                                                  50 push eax
68a3040000 push 000004a3
                                                                  e820f3ffff call 000004f2
                                                                                           add esp,+08
                                                                                          xor eax, eax
                                                                                           pop ebp
                                                                                           ret
 Number of Instructions Executed (1118) = 17 Pages
```

H correctly determines that P() never halts

```
void P(u32 x)
    if (H(x, x))
       HERE: goto HERE;
    return;
 int main()
    Output("Input_Halts = ", H((u32)P, (u32)P));
_P()
[00001202](01)
[00001203](02)
[00001205](03)
[00001208](01)
[00001206](01)
[00001206](05)
[00001212](03)
[00001215](02)
[00001215](02)
[00001219](02)
[00001216](01)
Size in bytes:
                                                        push ebp
                            8bec
                                                        mov ebp,esp
                            8b4508
                                                        mov eax, [ebp+08]
                            50
                                                        push eax
                            8b4d08
                                                        mov ecx, [ebp+08]
                                                       push ecx
call 00001032
                            e820feffff
                            83c408
                                                        add esp,+08
                                                       test eax,eax
jz 0000121b
                            85c0
                            7402
                            ebfe
                                                        jmp 00001219
                            5d
                                                        pop ebp
                                                        ret
 Size in bytes:(0027) [0000121c]
_main()
[00001222](01)
[00001223](02)
[00001225](05)
[0000122a](05)
[0000122f](05)
                                                        push ebp
                                                       mov ebp, esp
push 00001202
push 00001202
call 00001032
                            8bec
                            6802120000
                            6802120000
                            e8fefdffff
 [00001221] (03)
[00001234] (03)
[00001237] (01)
[00001238] (05)
[0000123d] (05)
                                                       add esp,+08
push eax
push 000003b3
call 00000402
                            83c408
                            68b3030000
                            e8c0f1ffff
 [00001236] (03)
[00001242] (03)
[00001245] (02)
[00001247] (01)
[00001248] (01)
                                                       add esp,+08
xor eax,eax
                            83c408
                            33c0
                                                        pop ebp
                            5d
                                                        ret
 Size in bytes:(0039) [00001248]
  machine
                   stack
                                     stack
                                                      machine
                                                                         assemblv
  address
                   address
                                     data
                                                      code
                                                                         language
 [00001222] [0010200f] [00000000]
[00001223] [0010200f] [00000000]
[00001225] [0010200b] [00001202]
[0000122a] [00102007] [00001202]
[0000122f] [00102003] [00001234]
                                                                         push ebp
                                                     8bec mov ebp,esp
6802120000 push 00001202 // push P
6802120000 push 00001202 // push P
e8fefdffff call 00001032 // call executed H
Begin Simulation
                                 Execution Trace Stored at:2120c3
Infinitely Recursive Simulation Detected Simulation Stopped
H knows its own machine address and on this basis it can easily
examine its stored execution trace of P (see above) to determine:
(a) P is calling H with the same arguments that H was called with.
(b) No instructions in P could possibly escape this otherwise infinitely recursive emulation.
(c) H aborts its emulation of P before its call to H is emulated.
 [00001234] [0010200f] [00000000]
[00001237] [0010200b] [00000000]
[00001238] [00102007] [000003b3]
[00001234] [00102007] [000003b3]
                                                     83c408
                                                                         add esp,+08
                                                     50 push eax
68b3030000 push 000003b3
                                                     e8c0f1ffff call 00000402
 Input_Halts = 0

[00001242][0010200f][00000000]

[00001245][0010200f][00000000]

[00001247][00102013][00100000]

[00001248][00102017][00000004]
                                                     83c408
                                                                         add esp,+08
                                                     33c0
                                                                        xor eax, eax
                                                     5d
                                                                         pop ebp
                                                                         ret
 Number of Instructions Executed(870) / 67 = 13 pages
```