

Proof that Wittgenstein is correct about Gödel

When we sum up the results of Gödel's 1931 Incompleteness Theorem by formalizing Wittgenstein's verbal specification such that this formalization meets Gödel's own sufficiency requirement: "Every epistemological antinomy can likewise be used for a similar undecidability proof." then we can see that Gödel's famous logic sentence is only unprovable in PA because it is untrue in PA because it specifies the logical equivalence to self contradiction in PA.

Wittgenstein's minimal essence of the 1931 Incompleteness Theorem sentence

"I have constructed a proposition (I will use 'P' to designate it) in Russell's symbolism, and by means of certain definitions and transformations it can be so interpreted that it says 'P is not provable in Russell's system'. (Wittgenstein 1956:50e)

Formalized by Olcott: $P \leftrightarrow (RS \neq P)$

Wittgenstein definitions of True() and False()

'True in Russell's system' means, as was said: proved in Russell's system; and 'false in Russell's system' means: the opposite has been proved in Russell's system.

(Wittgenstein 1956:51e) Formalized by Olcott as:

$\forall x (\text{True}(RS, x) := (RS \vdash x))$

$\forall x (\text{False}(RS, x) := (RS \vdash \neg x))$ // LHS := RHS means LHS is defined as the RHS.

When we understand that the body of conceptual knowledge is entirely comprised of stipulated relations between expressions of language then we realize that both true and provable are concurrently defined by these stipulated relations. This proves that the above predicates merely correspond to the way that conceptual true really works.

The fact that no counter-examples of conceptual truth (the analytic side of the analytic versus synthetic distinction) that are not defined by these stipulated relations exist proves that conceptual truth is only defined by these stipulated relations.

Since the Wittgenstein-Olcott axiom schema define $\text{True}(RS, x)$ as $\text{Provable}(RS, x)$ then $\neg\text{Provable}(RS, x)$ would be defined as $\neg\text{True}(RS, x)$. This means that the Wittgenstein-Olcott minimal essence of the 1931 Incompleteness Theorem <IS> The Liar Paradox.

The Formalized Liar Paradox says that P is materially equivalent to Not True.

The truth table shows that this is self-contradictory.

$P \leftrightarrow \neg\text{True}(P)$	$P \leftrightarrow RS \neq P$
T F F	T F F
F F T	F F T

The truth table of minimal essence of the 1931 Incompleteness theorem is identical to the truth table of the Liar Paradox because the third columns of these truth tables are stipulated by the Wittgenstein-Olcott axiom schema to mean exactly the same thing.

The failure of logical equivalence shows that both P and $\neg P$ are contradicted (false) (in the above formula) thus meeting the [epistemological antinomy] sufficiency condition that Gödel stipulated for proof equivalence:

“14 Every epistemological antinomy can likewise be used for a similar undecidability proof.” (Gödel 1931:40)

The fact that self-contradictory sentences specified in the language of a formal system cannot be proven in that formal system does not make the formal system itself incomplete or inconsistent as long as unprovable (from axioms) is construed as untrue.

Furthermore that the Gödel sentence can be proved to be unsatisfiable because its satisfaction would derive a contradiction proves that this sentence is unprovable.

The Gödel sentence is provably unprovable because this proof one level of indirection away from the original sentence, thus neither self-referential nor self-contradictory:

(a) “This sentence is not provable” is not true or provable.

(b) Provable(“This sentence is not provable”) is true and provable.

At the most abstract level of analysis:

Conceptual Truth is ONLY semantic relations between concepts that can always be expressed as[1] syntactic relations between finite strings[2] thereby logically entailing that truth cannot possibly ever diverge from provability.

[1] Forming a perfect isomorphism between semantic and syntactic relations

$\forall x (\text{True}(x) \cong \text{Provable}(x))$

[2] Such as words, word phrases or predicate logic expressions.

Examples:

"one" [is a] "Integer"

"cats" [are] "Animals"

"cats" [have] "legs"

"2 + 3" [equals] "5"

"A \wedge B" " \leftrightarrow " "B \wedge A"

To make the above abstraction more concrete we focus on the single relation between concepts of [sound deduction] from the sound deductive inference model.

Sound deduction begins with stipulated truth, applies a sequence of truth preserving operations, thus necessarily ends up with truth.

Truth ONLY comes from:

(1) Stipulated truth (the definitions of the meaning of words)

(2) Applying a sequence of truth preserving operations to stipulated truth.

Truth ALWAYS comes from:

- (1) Stipulated truth (the definitions of the meaning of words)
- (2) Applying a sequence of truth preserving operations to stipulated truth.

When we construe a formal systems axioms to essentially be stipulated truth then this same formal systems theorems would also be true because they were derived by applying truth preserving operations to its axioms. Since this is the way that Truth really works we have proven that true can never diverge from provability.

Godel, Kurt 1931 On Formally Undecidable Propositions of Principia Mathematica And Related Systems I, page 40.

Wittgenstein, Ludwig 1956 Remarks on the Foundations of Mathematics Part I, Appendix I Paragraph 8, pages 50e-51e.

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