Rebutting the Sipser Halting Problem Proof

A simulating halt decider computes the mapping from its input finite strings to an accept or reject state on the basis of the actual behavior specified by this input as measured by its correct simulation of this input. The following shows how the correct value for the D and (D) diagonal in Sipser's Figure 4.6 is accept.

We start with Sipser's definitions of H and D:

On input (M, w), where M is a TM and w is a string, H halts and accepts if M accepts w. Furthermore, H halts and rejects if M fails to accept w. In other words, we assume that H is a TM, where

```
H((M,w) = { accept if M accepts w
{ reject if M does not accept w
```

••

Now we construct a new Turing machine D with H as a subroutine. This new TM calls H to determine what M does when the input to M is its own description (M). Once D has determined this information, it does the opposite. That is, it rejects if M accepts and accepts if M does not accept.

```
D(\langle M \rangle) =  { accept if M does not accept \langle M \rangle { reject if M accepts \langle M \rangle (Sipser 1997:165)
```

We encode the Sipser D and define the behavior of Sipser H as C functions.

```
/// H returns 1 when its input would halt and return 1.
// otherwise H returns 0
//
int Sipser_D(ptr2 M)
{
   if ( Sipser_H(M, M) )
      return 0;
   return 1;
}
int main()
{
   Output((char*)"Input_Halts = ", Sipser_D(Sipser_D));
}
```

Complete halt deciding system (Visual Studio Project) Sipser version.

- (a) x86utm operating system
- (b) x86 emulator adapted from libx86emu to compile under Windows
- (c) Several halt deciders and their sample inputs contained within Halt7.c https://liarparadox.org/2022_10_08.zip

D calls simulating halt decider H which computes the mapping from its input D to an accept or reject state on the basis of its correct simulation of D. When H correctly determines that this simulated input would remain stuck in recursive simulation H aborts this simulation and reports non-halting by returning 0. When D reverses this decision it returns 1. This is used to correctly fill in the "?" in the Sipser Figure 4.6 with "accept".

Simulating halt decider H recognizes instances of recursive simulation using the same criteria that it uses in its dynamic behavior pattern that recognizes infinite recursion:

```
void Infinite_Recursion(u32 N)
  Infinite_Recursion(N);
}
        \langle M_1 \rangle
                   \langle M_2 \rangle
                              \langle M_3 \rangle
                                        ⟨M₄⟩ . . .
                                                   ⟨D⟩ . . .
   M_1 accept
                   reject
                             accept
                                         reject
                                                    accept
   M₂ accept
                             accept
                                         accept
                                                    accept
                   accept
   M₃ reject
                   reject
                             <u>reject</u>
                                         reject
                                                    reject
   M₄ accept
                                                    accept
                   accept
                             reject
                                         <u>reject</u>
                                                    ?__
        reject
                   reject
                              accept
                                         accept
   D
   Figure 4.6 (Sipser 1997:167)
```

Sipser, Michael 1997. Introduction to the Theory of Computation. Boston: PWS Publishing Company (165-167)

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