## NOTE ON DEDUCTIVE INFERENCES Draft of August 02, 2024 Matheus Silva

In relation to inferences, there is a tendency to conflate alethic with epistemic modalities:

## **Material implication**

- 1. It's not the case that B is false and A is true in a given world. (alethic claim)
- 2. It's certain that B isn't false and A is true in a given world. (epistemic claim)

## **Formal implication**

(1\*) It's not the case that B is false and A is true in any possible world. (alethic claim)

(2\*) It's certain that B isn't false when A is true in any possible world. (epistemic claim)

But notice that (2) doesn't follow from (1), and ( $2^*$ ) doesn't follow from ( $1^*$ ). Now, suppose one asserts (1) because it is highly likely. In this case, there would be no meaningful distinction between (1) and the non-deductive inference:

 $(1^{**})$  It is unlikely that A is true and B is false in a given world.

This suggests that the main reason to distinguish deductive from non-deductive inferences lies in epistemic modalities, but what determines whether an inference is deductive or not are its alethic commitments. In other words, the supposed non-deductive status of an inference is simply an epistemic element that should be irrelevant from a logical point of view—unless the goal is to express reasoning about knowledge and belief.

The same could be said about patterns of coherence requirements for inferences such as *modus ponens* and hypothetical syllogism. They track the consequences of alethic truths and not our epistemic commitments.