The price of inscrutability

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In our reasoning we depend on the stability of language, the fact that its signs do not arbitrarily change in meaning from moment to moment. (Campbell, 1994, p.82)

Some philosophers offer arguments that ordinary names such as “London” are radically indeterminate in reference. The conclusion of such arguments is that there is no fact of the matter whether “London” refers to a city in the south of England, or whether instead it refers to Sydney, Australia.

Some philosophers have even suggested that we accept the conclusion of these arguments. Such a position seems crazy to many; but what exactly goes wrong if one adopts such a view? This paper evaluates the theoretical costs incurred by one who endorses extreme inscrutability of reference (the ‘inscrutabilist’). I argue that there is one particular implication of extreme inscrutability which pushes the price of inscrutabilism too high. An extension of the classic ‘permutation’ arguments for extreme inscrutability allow us to establish what I dub ‘extreme indexical inscrutability’. This result, I argue, unacceptably undermines the epistemology of inference.

The first half of the paper develops the background of permutation arguments for extreme inscrutability of reference and evaluates some initial attempts to make trouble for the inscrutabilist. Sections 1 and 2 describe the setting of the original permutation arguments for extreme inscrutability. Sections 3 and 4 survey four potential objections to extreme inscrutability of reference, including some recently raised in Vann McGee’s (2005a). Sections 5 sketches how the permutation arguments can be generalized to establish extreme indexical inscrutability; and shows how this contradicts a ‘stability principle’—that our words do not arbitrarily change their reference from one moment to the next—which I claim plays a vital role in the epistemology of inference.

The second half of the paper develops in detail the case for thinking that language is stable in the relevant sense. In section 6, I use this distinction to call into question the epistemological relevance of validity of argument types. In section 7, I argue that stability is exactly what is needed to fix the puzzle, and so secure the relevance of validity to good inferential practice. Section 8 responds to objections to this claim.

An appendix to the paper provides formal backing for the results cited in this paper, including a generalization of permutation arguments to the kind of rich setting required for a realistic semantics of natural language. Extreme indexical inscrutability results can be proved within this setting.

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I

1 Inscrutability Arguments and Interpretationism

I take positive inscrutability arguments to have the following form:

1. **Sentential Constraints**: The sole criterion of success for a semantic theory is that it assign the right semantic value to sentences: if two semantic theory both assign all the right semantic values to sentences, then it is indeterminate which one is correct.

2. **Overgeneration**: Multiple assignments of subsentential reference generate the right semantic values at the level of whole sentences.

3. **Therefore Inscrutability**: It is indeterminate what subsentential expressions refer to.

Whether or not **Overgeneration** holds is a technical question, amenable to formal proof or disproof. **Sentential Constraints**, on the other hand, is a distinctive and controversial thesis in the philosophy of linguistic representation (the discipline sometimes called ‘foundational semantics’, ‘metasemantics’, ‘the theory of meaning’ etc).

**Sentential Constraints** has been endorsed in one form or another by many theorists, including David Lewis (1975), Donald Davidson (1974; 1977; 1979), Hilary Putnam (1980) and W. V. Quine (1960). The basic thought is a natural one: it is at the level of whole sentences that language most directly makes content with the states of affairs that it is its job to represent. We assertorically utter sentences to say that thus-and-such a state of affairs obtains: and this is manifest in a correlation between occasions of uttering whole sentences, and the states of the world on that occasion.2

The idea of Quine, Lewis, Davidson, Putnam and others is that from this correlation between sentences and states of the world one may extract information about what kind of semantic values sentences can have. Semantic theory as a whole is constrained to fit this sentential semantic data. This is the view encapsulated in **Sentential Constraints**.

The theorists differ amongst themselves as to how the extraction of sentential semantic data is carried out; and over the form in which the data is to be presented. Some examples: the simplest view formulates the data simply as assignment of truth-values to sentences. Sentences are paired with the True just in case they are the ones that ordinary speakers assent to.3 Equivalently, one might collect the sentences paired with ‘the True’ into one big set: what Lewis (1984) calls ‘total theory’. **Sentential Constraint** then becomes the requirement that correct semantic theory make-true (so far as possible) this one big theory. This package is known as ‘global descriptivism’.

More sophisticated alternatives include Davidson and Lewis’s respective versions of ‘radical interpretation’. For Davidson, the sentential data is to be formulated as the set of ‘T-sentences’ (e.g. ‘schnee est weiss’ is true iff snow is white). There is a complex story about how the radical interpreter fixes on a set of T-sentences in the course of finding an overall theory that best explains the behaviour of her subjects. Lewis (1975) offers yet another package. The sentential data is this time to be formulated as a pairing of propositions (sets of possible worlds) with sentences, where the pairing is extracted from information about conventions of truthfulness and trust prevailing in a community. In all the cases mentioned, there is the distinctive second stage: semantic theory is constrained solely to match the sentential data, however it might be formulated.4
This style of foundational theory of linguistic representation (‘metasemantic’ theory) I call interpretationism. On all the versions of interpretationism currently in view, Sentential Constraints will be sustained. On others it may not be. To see this, let’s further break Sentential Constraints down into two distinct theses:

1. **Sentential Data**: The data-set constraining the selection of semantic theory concerns the semantic values of sentences—e.g. a set of T-sentences, or a pairing of sentences with propositions.

2. **Best=Fit**: The sole criterion of success for a semantic theory is fitting this data: if two theories both optimally fit the data, it is indeterminate which is correct.

In response to the inscrutability arguments to be discussed below, many sympathetic to interpretationism look to avoid Best=Fit. A famous example is Lewis (1983, 1984). Lewis describes semantic theories as more or less eligible to the extent that the semantic values they assign to words are natural (so the thought is that all else equal, an interpretation that assigns *green* to a word, is more eligible than one that assigns ‘grue’ to that same word.) Lewis then argues within the context of a broadly interpretationist metasemantics, that the meaning-giving interpretation, as well as getting the semantic values of whole sentences optimally right, also needs to be optimally eligible. These complications to the interpretationist picture are not our topic here.

Given Sentential Constraints, to argue for the extreme inscrutability, it suffices to show that given a ‘sensible looking’ semantic theory for English, we can construct another one that:

1. Assigns the same semantic values to whole sentences.

2. Embeds arbitrarily crazy scheme of reference to singular terms

The famous ‘permutation arguments’ show us that such overgeneration results are indeed available.

## 2 Permutation arguments

The key idea of permutation arguments is that twisted assignments of extensions (referents) to constants are compensated by equally twisted assignments of extensions to predicates. Overall, the twists ‘cancel out’ to deliver the usual result at the level of sentences. For a toy example of this, let us use the phrase ‘the image of x’ to pick out x whenever x is anything other than Billy or the Taj Mahal; to pick out Billy if x is the Taj Mahal; and to pick out the Taj Mahal if x is Billy. We can describe our twisted reference scheme as follows: $N$ twist-refers to x iff $N$ standardly-refers to $y$ and x is the image of y. For the similarly twisted assignment of extensions to predicates, take any atomic predicate $P$. Let $P$ twist-apply to x iff $P$ standardly applies to some $y$, such that x is the image of y. The twists cancel out—the distribution of truth-values to sentences is the same on both interpretations. For example, “Billy is running” is true iff the referent of “Billy” falls under the extension of “runs”. The twist-referent of “Billy” is the Taj Mahal; but the twist-extension of “runs” includes all the images of running things. Since Billy runs, and the Taj Mahal is the image of Billy, the Taj Mahal falls under the twist-extension of “runs”. The sentence comes out true, just as it does under the standard interpretation. By induction, we are able to show that this generalizes to arbitrary truth-functional compounds.

The above sketch gives the root idea of permutation arguments: twists in one area of sub-sentential content ‘cancelling out’ others. To provide an inscrutability argument for English,
however, we would need to argue that such a result goes through for a semantic theory ade-
quate for the richness and complexity of syntactic structure we find in that language. Further,
for full generality, we should show not only that permutation arguments preserve truth values
but whatever entities are assigned as semantic values of sentences. The fullest presentation of
these results of which I am aware still only proves the result for a framework that is expres-
sively limited in comparison to the multiply intensional type theory used by linguists in the
Montague tradition. In an appendix to this paper, I provide a more general result: I show that
the permutation results hold within the ‘general semantics’ framework of Lewis (1970).

3 The costs of extreme inscrutability of reference

Interpretationism is an attractive theory of how facts about linguistic representation can be fixed
by facts about patterns of assent and dissent (facts that are do not themselves have to be char-
acterised in semantic terms). In the form presented above, interpretationism is a very clean and
simple theory. Yet it apparently implies extreme inscrutability of reference: there is no fact of
the matter about whether “Londres” refers to London or to Sydney.

One reaction at this point would be to start tweaking the content of interpretationism: dropping
the idea that the sole constraint on the success of semantic theory is that it ‘fit data’ about
the semantic values of whole sentences (what we earlier called BEST=FIT). Such additions
increase the complexity of interpretationism: for example, on Lewis’s preferred version, men-
tioned earlier, we will need a (non-semantic) account of what it takes for macroscopic properties
to be eligible or natural; we also require some explication of how to weigh up considerations
of fit against considerations of eligibility.

I do not wish to rule out the tenability of some such tweaked version of interpretationism,
especially if the impression that the additional constraints are ad hoc monster-barring moves
can be ameliorated. But getting the tweaks right is no easy task. (I argue in (2007) that Lewis’s
response fails unless we accept a radically ‘emergent’ ontology of fundamental properties.)

To start altering the theory may be an overreaction. There is much to gain if we could ‘bite
the bullet’ and simply accept that reference is inscrutable: we gain a clean and simple theory
of linguistic representation, and at what cost? Certainly some counterintuitive results. But (one
may think) philosophers have learned to live with worse.

As already mentioned, Davidson (1977, 1979) is one such figure. On his view, commitment
to extreme inscrutability is an insight of interpretationism, not a problem for it. The central
purpose of the remainder of this paper is to examine whether this is a tenable proposal. We shall
be looking at the costs of inscrutability of reference. In the end, I shall argue, inscrutability of
reference poses unsurmountable problems for our theory of inferential practice. To emphasise:
it is not my aim here to show where the argument for inscrutability goes wrong, if it does: it is
to determine whether or not we are obliged to find some flaw in it.

Before turning to detailed considerations, however, we should distinguish between two
forms of inscrutability thesis one might argue against in this way. For example, consider the
English expression “Rabbit”. Arguments for moderate inscrutability aim to establish that there is
no fact of the matter which of a range of entities this word applies to. Famously, Quine’s “argu-
ment from below” (1950, ch.2) aimed to establish that there is no fact of the matter whether ‘rab-
bit’ applies to rabbits, instantaneous rabbit-stages, or undetached rabbit-parts. McGee (2005a)
argues that Unger’s (1980) ‘problem of the many’ should be seen as establishing a similarly
moderate form of inscrutability: there is no fact of the matter which entity the name “Kiliman-
jaro” picks out, though whatever it picks out will be a mountain-like agglomeration of rock in
the vicinity of that mountain. Some think that the vagueness of much of natural language should
be analyzed as consisting in a (moderate) form of inscrutability.

Contrasted with this putative moderate inscrutability, the form of inscrutability that the permutation argument targets is extreme. An extreme inscrutability thesis might say that there is no fact of the matter whatsoever which entities ‘rabbit’ applies to, or what ‘Kilimanjaro’ picks out. This extreme inscrutability thesis holds that Paris and Sydney, and small furry creatures orbiting distant stars, have as much claim as any city in the south of England to be the referent of “London”. It is not determinately the case that ‘London’ doesn’t refer to them. The permutation arguments accepted by Davidson and others purport to establish this extreme form of inscrutability.

My focus in this paper will be on extreme inscrutability results, and the costs of accepting that reference is inscrutability in the extreme way. But I will also consider whether the considerations I bring against extreme inscrutability are also reasons for rejecting moderate inscrutability. On the one hand, a successful argument for the determinacy of reference (against moderate or extreme inscrutability) would be a surprising and significant result. On the other hand, an argument that impacts only on extreme inscrutability, while leaving moderate inscrutability untouched, arguably identifies the distinctive costs of the interpretationist metasemantic setting. Either way, therefore, it is worth considering the scope of the arguments we consider.  

4 Objections to inscrutability

In this paper, I will be largely focussed on investigating one particular cost of extreme inscrutability: its damaging interaction with the idea of good token inferences. But one might suppose that there were other, quicker objections to be had. So I begin by briefly mentioning some potential candidates, to flag up what I take to be problematic about them.  

The incredulous stare  The thesis under consideration is quite extraordinary. Hold up a red ball in front of your face. Say aloud “that red ball is shiny”. Accompany the words by jabbing your fingers into the ball to remove any reasonable way of mistaking your intent. What is being claimed is that nevertheless, the words “that red ball” might just as well refer to the Taj Mahal as to the red, shiny ball in front of you. Isn’t that just unbelievable? Moreover, the claims denied seem obvious truisms: it denies ‘disquotational’ reference principles such as ‘ “London” refers to London’.

For languages in general, and in particular for the reference of one’s own language, arguments for extreme inscrutability seem to try to deny the non-negotiable. Lewis (1983, p.46) describes the principle that “Our language does have a fairly determinate interpretation” as “a Moorean fact”—one which we have more reason to believe, than we have justification for believing any premisses that might undermine it. For these, and other reasons, one might think that extreme inscrutability thesis is literally incredible.

Notice that the incredulity here is directed at extreme inscrutability theses. Moderate inscrutability—such as that purportedly generated in the problem of the many, or in obscure mathematical cases—does not, I think, generate quite such intuitive repulsion. Some, indeed, have felt something the purported limited inscrutability of ‘rabbit’ for which Quine argues is incredible; elsewhere (minga) I argue that this is an artefact of the way the Quine’s argument is typically presented, and that the conclusion should not considered all that surprising. The objection by incredulous stare, therefore, is particular to the case of extreme inscrutability.

Underminingness  One might suspect that accepting extreme inscrutability undermines the very argument we give for it. If the theorist’s language is itself inscrutable in reference,
it may be thought mysterious how we conceive of and discriminate between various rival interpretations of our language. In particular, are we not supposing that there is an ‘intended’ interpretation of the language, from which our ‘deviant’ interpretations are parasitically constructed? If so, doesn’t the conclusion of the inscrutability argument undermine the argument given for it?

Again, we can ask the same question about moderate inscrutability theses: are they damagingly undermining? Of course, whether there’s a prima facie case to answer depends on what exactly the argument is for this moderate inscrutability, that might be ‘undermined’ by the conclusion. (The most plausible case that I know of is that of indeterminacy of quantification arising from the Lowenheim-Skolem arguments as deployed by e.g. Putnam (1980). For to give an argument that one’s unrestricted quantifiers are inscrutible in range between $D_1$ and $D_2$, it looks like one has to allow oneself the resources to quantify over the union of these sets! And the conclusion of the argument is that it is not determinately the case that one can do this.)

Semantic beliefs A traditional view in philosophy is that linguistic competence is a matter of knowledge of the meaning of expressions (or perhaps some related attitude). Call these cognitive approaches to understanding. It might be thought that extreme inscrutability (to its discredit) rules out a cognitive account of understanding.

The kind of cognitive approach to understanding that may be in tension with extreme inscrutability is one where we have to have knowledge, not only of what sentences express, but also what words within sentences express. On this ‘strong’ cognitive conception of understanding, in understanding a sentence containing the name $N$ we must at least believe something of the form:

\[ N \text{ refers to } o \]

or perhaps, for appropriate descriptive content $F$:

\[ N \text{ refers to something which is } F \]

Extreme inscrutability says that there is never any fact of the matter about whether such claims hold good. Prima facie, the upshot will be that one’s understanding will consist in part in beliefs whose contents are indeterminate. And this seems to lead the inscrutabilist into Moorean paradoxical situations: she holds $p$ to be indeterminate, but nevertheless (as part of her linguistic competence) believes that $p$. This seems to disclose a form of irrationality in the inscrutabilist stance.

Does the moderate inscrutabilist face parallel worries? If we insist that linguistic competence in $N$ is partially constituted by the semantic belief that $N$ refers to $o$ then they are in the same situation as the extreme inscrutabilist: being committed to beliefs which are indeterminate in content. Under this assumption, moderate and extreme inscrutability stand and fall together. However, under a slightly more relaxed version of the strong cognitive approach to understanding, the semantic belief that in part underlies our understanding of ‘Kilimanjaro is big’ can be something like: ‘Kilimanjaro’ refers to some mountain-like agglomeration of rock located in Southern Africa, larger than any other distinct mountain-like agglomerations of rock in that continent. On the sort of moderate inscrutability generate by ‘problem of the many’ considerations, the descriptive content here invoked may determinately apply to all of the candidate referents for ‘Kilimanjaro’ (in the extreme inscrutability case, of course, any such predicate would have to apply to
absolutely every object!). So, absent arguments that the strong cognitive conception has to take the more severe form, there is no general tension between moderate inscrutability theses and the strong cognitive conception of understanding.

**Inscrutability of rigidity and existence**  Vann McGee (2005a) has recently put forward a range of considerations intended to show that the permutation arguments for inscrutability break down when we consider more than just the expressively impoverished setting of extensional first order logic. An appropriate rejoinder is to show that the arguments do go through in as rich a setting as one could want. This is done in the appendix to this paper.

Though I do not think that McGee’s arguments provide formal obstacles to the inscrutabilist, I think they show something really interesting about the commitments of the inscrutabilist.

McGee considers permutation arguments in the setting of quantified modal logic (like him I assume familiarity with standard possible worlds semantics for such systems). Now, it is commonly (though not universally) held that what exists in one world can fail to exist in another. Suppose that to be the case. When deploying one’s permutation argument one can either (a) look at the domain of possibilia as a whole, and let one’s permitted interpretation be based on the a permutation of possibilia irrespective of which worlds they exist at; or (b) take the domain of each world in turn, and permute the extensions of expressions at world w where the each such permutation is restricted to objects that exist within its respective world. Either way, McGee thinks there is trouble.

On strategy (a), suppose that the ‘overall’ permutation maps possibulum a to possibulum b, and that on the intended interpretation of our language the rigid designator ‘Billy’ is a name for a. Then (absent necessary connections between a and b) there will be a world w where a exists and b does not. On the intended interpretation, ‘Billy’ denotes a at w; and consequently on the permuted interpretation, ‘Billy’ must denote b at that world. But b doesn’t exist even exist in w!

To dramatize this, suppose that w is the actual world, and ‘Billy’ a name in English. Then the permuted interpretation has it that ‘Billy’ names something that doesn’t actually exist; and absent special pleading, the inscrutabilist has to say that there is no fact of the matter whether or not our ordinary proper names designate non-existent entities.

On strategy (b), we are forced to choose different permutations at different worlds. On this strategy the intension of ‘Billy’ will be a function mapping a world w to the image of a under the permutation chosen for w. Suppose a is mapped to b by the chosen permutation for the actual world. Then (on the assumption that there is no necessary connection between a and b) take a world w where a exists but b does not. The chosen world-restricted permutation for w obviously can’t send a to b. So it must send a to something else, c say. So the two permutations disagree on what a is mapped to. Again, suppose ‘Billy’ names a according to the intended interpretation. On the permuted interpretation, the extension of ‘Billy’ at the actual world will be b, and the extension of ‘Billy’ at w will be the distinct object c. Thus, absent necessary connections between individuals, any “permuted alternative” to the sensible interpretation the ordinary proper name ‘Billy’ will turn out to be non-rigid. If such deviant interpretations cannot be excluded by interpretationist lights, we get not only extreme inscrutability, but also inscrutability over whether or not ordinary proper names are rigid designators.

McGee’s arguments seem particular to the case of extreme inscrutability: there is no obvious way to construct parallel concerns for the moderate inscrutabilist.
We have just seen a number of challenges to inscrutability, and to extreme inscrutability in particular. Notice that, in accordance with the spirit of this paper, none attempts to describe what goes wrong with the permutation argument.\footnote{11}

I am dissatisfied by each of the above putative objections to the inscrutabilist. I do not have space here to discuss each in detail, I will briefly mention the shape of my concern in each case.\footnote{12}

There is a track record in philosophy of influential views that generate incredulous stares: David Lewis’s extreme modal realism; Timothy Williamson’s epistemicist theory of vagueness; Graham Priest’s defence of true contradictions, Peter Van Inwagen’s denial of the existence of medium sized dry goods. But in each case, their opponents seek objections beyond the incredulous stare, and with good reason.

If one’s only grounds for complaint against a theory is that it is literally incredible, then one is in a dialectically weak position when faced with someone who, in all seriousness, advocates the position. Such an inscrutabilist may fairly object that the psychological limitations exhibited in your finding the position literally unbelievable should be of no concern to them. (And, recall, the ‘extreme inscrutabilist’ is no mere fiction: Donald Davidson accepts this position.)

Perhaps, though, the emphasis should not be on the ‘literal unbelievability’ of extreme inscrutability. Rather, we should focus on its counterintuitiveness or ‘Moorean’ status. Even the convinced inscrutabilist may admit that it is some cost to their theory that they go against common sense in these ways. But with what right do we suppose that the discredit this earns the inscrutabilist position outweigh the benefits that the position makes available? I can only speak for myself, but the interpretationist promise of a reductive account of the representational properties of language would be, for me, a big enough benefit to compensate for some departures from pre-theoretic opinion were there to be no independent problems with the view, and were I able to bring myself to believe in it.

Were I to endorse inscrutabilism, I would seek to ameliorate the embarrassment of disagreeing with pre-theoretic opinion by attempting to ‘explain away’ intuitions against inscrutabilism. I might, for example, point to the fact that one can introduce into the object language devices that obey the disquotational rules for ‘truth’ and ‘reference’ respectively. I would carefully distinguish these purely disquotational notions from the heavyweight world-word relations that the interpretationist seeks to give an account of. Accepting extreme inscrutability for the representational notion of ‘reference’ is not to debar oneself from talking-the-talk of disquotational reference.\footnote{13}

The idea that adopting the thesis of inscrutabilism renders problematic the arguments given for accepting it is intriguing. It is extremely sensitive to the exact nature of the arguments for inscrutabilism given: with the putative moderate inscrutability of unrestricted quantification being a promising case. The question is: do the permutation arguments for extreme inscrutability have such a form? Admittedly, permutation arguments for inscrutability are often presented by talking about an ‘intended’ interpretation, and derivatively constructing deviant interpretations. That naturally leads to the thought that absent an ‘intended’ interpretation they will be ill-formed. However, the appearances mislead. We should simply note that we never need to pick out individual interpretations in giving the argument—not even an ‘intended one’. Rather, we just argue for the conditional claim that, for all $x$, if $x$ is an interpretation-function which renders true a set of sentences $T$, then a permuted variant of $x$ also renders this true.\footnote{14} We then need only the principle that there is some interpretation which gets the sentential data right, to conclude to extreme inscrutability.\footnote{15} I conclude that these considerations fail to cause trouble for the inscrutabilist.

The putative tension between strong cognitive accounts of understanding and extreme inscrutability is a promising route. Indeed, I think that, aside from the approach explored at
length here, this is the most promising way to argue against extreme inscrutability. It is important to note that the claim that linguistic competence in part consists of something like beliefs about subentential meaning is itself highly controversial. So no knock down blow can be expected here. Elsewhere (Williams, 2005, ch.6), I have argued that the inscrutabilist can resist the objection directly: by considering carefully potential correlative indeterminacies between the content of thought and the content of language, we are able to resist the argument that the semantic beliefs needed for the strong cognitive conception of understanding are indeterminate.

That leaves us with the McGee-inspired costs: the result that (depending on how we extend the permutation arguments) we are faced either by what we might call the inscrutability of rigidity, or the inscrutability of existence. Let me immediately note that this assumes that the domains of worlds vary: that things go in and out of existence from world to world. This is certainly deniable. Setting that line of resistance aside, notice that the considerations mentioned at best show that the inscrutabilist is committed to one or other of the inscrutability of existence or the inscrutability of rigidity. They do not show what is wrong with being committed to one or other of these results. Extreme inscrutability is already highly counterintuitive: what we have been shown is other, similarly counterintuitive consequences of the position. But again, is the alleged badness of these commitments of the inscrutabilist position simply that they generate an incredulous stare (in which case, we’ve made no progress, since extreme inscrutability alone does that!). Or are there more detailed considerations to be found against them?

It is true that the rigidity of proper names is philosophical orthodoxy, and it is natural to hope to find, in the arguments that established this orthodoxy, grounds for objecting to the inscrutabilist who holds that it is indeterminate whether proper names are rigid. But the evidence for this claim, I take it, largely consists of data about the truth-conditions of various sentences (such as ‘Aristotle could have died at birth’). But of course the (non-rigid) permuted interpretations match the ‘intended’ one at the level of truth-conditions of whole sentences. So there simply isn’t going to be any data of this kind that tells against non-rigidity in this peculiar form.

What about the inscrutability of existence? Is there something untenable about the thesis that one refers to (contingently) non-existent things? Notice that it cannot be a problem over words standing in relations to non-existent relations as such that is at issue: for on the kind of modal semantic framework that is being assumed, the semantic values (intensions) of predicates such as ‘is self-identical’ will be sets that contain mere possibilia within their transitive closure. So semantic relations already relate words to entities of provenance at least as dubious as possibilia themselves. Why should the semantic relation of reference be any different?

But once the ontology worry about relating-to-the-ontologically-dubious are set to one side, it is hard to see what the remaining worry is. Consider a temporal analogy. We can refer to Beethoven, even though he does not exist at the present time. Likewise, the current extension of ‘famous’ contains presently non-existent things, for Beethoven is currently famous. Such examples show, I take it, that some words refer relative to a time, to things that fail to exist at that time. Why should the relativization to worlds be any different?

(Quite independently of the current considerations, some philosophers have argued that reference to mere possibilia can be achieved. Salmon (1998) invites us to consider the merely possible person who would have developed from this egg and this sperm, had they fused and developed. He argues that (granted certain essentialist assumptions) we introduce a name for this merely possible person. Far from being impossible, reference to the non-existent is arguably actual.)

The working assumption shall therefore be that none of the above provide cogent arguments against the extreme inscrutabilist. I therefore turn to considerations that do seem to me to promise to show why extreme inscrutabilism is untenable.
5 Inscrutability, Context and Validity

Extreme indexical inscrutability

What is required of a semantic theory by sentential constraints is simply that it assign the right semantic values to sentences. And we have already seen a recipe for constructing semantic theories embedding arbitrarily permuted reference schemes, that are sententially equivalent to ‘intuitively correct’ semantic theory.

However, we need not stop here. Given sentential constraints, we have all the resources we need to prove an even more general inscrutability result than the extreme inscrutability theses previously mentioned: extreme indexical inscrutability. This says that not only is there no fact of the matter as to whether ‘London’ refers to London or to Paris, but there is no fact of the matter whether or not it changes from referring to London, to referring to Paris, from one moment to the next.

One might wonder why indexical inscrutability doesn’t follow immediately from simple inscrutability. There is some prima facie appeal to the following argument:

1. It is indeterminate whether $e$ denotes $o$ in context $c$;
2. It is indeterminate whether $e$ denotes $o$ in context $c'$;
3. Therefore It is indeterminate whether ($e$ denotes $o$ in context $c$ and $e$ denotes $o$ in context $c'$)

Since we can run this argument for any object $o$, it looks like this form of argument can establish the inscrutability of co-reference across contexts, directly from the standard inscrutability of reference.

The form of inference, however, is fallacious: the logic of ‘determinately’ simply doesn’t work that way. Here is an argument of similar form:

1. It is indeterminate whether ‘Billy’ denotes the Taj Mahal;
2. It is indeterminate whether ‘Billy’ denotes the Eiffel Tower;
3. Therefore It is indeterminate whether (‘Billy’ denotes the Taj Mahal and ‘Billy’ denotes the Eiffel Tower)

The extreme inscrutabilist again grants both premises. But of course they reject the conclusion: they agree with orthodoxy that determinately a name picks out just one thing. This illustrates that indeterminacies can be coordinated in a way that blocks the form of inference that might get us quickly from extreme inscrutability to extreme indexical inscrutability. So more work is needed.\(^{21}\)

The detailed case for extreme indexical inscrutability is built from the permutation arguments previously sketched, and in broad outlines is as follows.\(^{22}\) First of all, we require a semantic theory that in principle allows words to vary in reference from one context to the next. But we need this in any case, since some words (‘I’ and ‘you’ and ‘them’, etc) do display such features. The standard Montagovian treatment of the phenomenon is to let the semantic value of a lexical item be a function from contexts to intensions. Thus, ‘I’ will be assigned a semantic value that takes contexts where Billy utters the word to the intension that is a constant function from worlds to Billy; and which takes contexts where Sally utters the word to the intension that is a constant function from worlds to Sally.
Suppose we take two ‘permuted’ semantic theories constructed in pursuance of the original inscrutability result, θ₁ and θ₂. These will each assign to expressions functions from contexts to intensions, which embed arbitrary crazy actual-world-reference schemes. In particular, suppose that θ₁ represents ‘Billy’ as referring to the Taj Mahal (no matter what the context is) and θ₂ represents ‘Billy’ as referring to the Great Wall of China (no matter what the context is).

Take any two contexts (say, the context in which I write these words, and the context in which you read them). The idea is then that we ‘cut and shunt’ these two interpretations to construct a third one, Θ, that will represent ‘Billy’ as referring to the Taj Mahal in the former context, and as referring to the Great Wall of China in the latter. In short, unlike θ₁ and θ₂, it represents Billy as an indexical expression, and one that shifts its reference over the (arbitrarily chosen) context-change.

How do we do this? Simply by considering the set of all possible contexts, C. This contains, in particular, the context c₁ in which I am writing, and the context c₂ in which you are reading. It will suffice to say what intensions Θ assigns to words at each point in C. So divide C exhaustively into two subsets, C₁, containing c₁, and C₂, containing c₂. Then say that the intension assigned by Θ to a word in a context c in C₁ are exactly those assigned to it in c by θ₁; and the intension assigned by Θ to a word in a context c in C₂ are exactly those assigned to it in c by θ₂. One can quickly check that this recipe means that ‘Billy’ will behave (according to Θ) exactly in the indexical way described above.

To argue from sentential constraints that Θ is a semantic theory which isn’t determinately incorrect, we need to make sure that at Θ fits with the all the sentential data the interpretationist can lay down. We secure this result because of the way Θ was constructed out of two interpretations which (ex hypothesi) already meet this condition. No matter which context we choose, either the semantic content assigned by Θ to all of the lexical items will match that assigned by θ₁ or the semantic content assigned by Θ to all of the lexical items will match that assigned by θ₂. By the compositionality of language, the intension of the sentence (in that context) is determined by the intension of its lexical parts (in that context). So in any context, Θ will assign to sentences intensions that match those assigned by θ₁ or by θ₂. But we are supposing that at the level of sentences, both these semantic theories match each other and fit with all the data the interpretationist can lay down. Hence the compound theory is sententially equivalent to θ₁ and θ₂: the interpretationist cannot declare it determinately incorrect.23

The upshot is that for any name n, and any pair of contexts c, c′, a compound theory fitting the interpretationist’s sentential data can be constructed, so that the reference assigned to n changes from c to c′. And, by interpretationist lights, there is nothing to make this compound theory determinately ‘unintended’. Thus, extreme indexical inscrutability follows: it is never determinately the case, from one context to the next, that the reference of a name remains the same.

Extreme indexical inscrutability requires only a minor extension of the original permutation arguments for extreme inscrutability of reference. If an interpretationist subscribes to extreme inscrutability on these grounds, she is in no position to resist my argument for extreme indexical inscrutability. As we shall see, the price extracted by extreme indexical inscrutability is high.

Good inference and context

Consider the following schematic claim:

**Stability**

For the set of contexts C (with at least two elements), and the non-null set of expressions E, the extension of each expression in E is the same at each context in C.
Extreme inscrutability, I have argued, will generalize to extreme indexical inscrutability. And it should be clear that extreme indexical inscrutability entails that no instance of STABILITY is better than indeterminate in status.

The second half of this paper is concerned to measure what costs are incurred in giving up all instances of STABILITY. We shall focus on the standing of certain token inferences which are of a logically valid type: arguments such as ‘Annie is female; Jen is female; so Annie and Jen are female’. Such arguments typically enjoy logical good standing: they have a distinctive (and arguably more impressive) epistemic status than arguments that are of an inductive form (all observed students are female; so all students are female); or which are backed only by entailments rather than logical validities (this is water; so this is H$_2$O). I will argue that if a token argument to be in logical good standing, the expressions involved in the argument must be stable across the contexts involved in the token argument. Thus, if all instances of stability are given up, no token argument will ever be (determinately) in logical good standing.

We can turn this into an explicit argument against extreme inscrutability, which forms the ‘master argument’ of this paper. The first premise says that some token argument $A$ is (determinately) in a logical good-standing. The second premise says that (determinately) any argument in logical good-standing contains only expressions whose content is ‘stable’ in the sense articulated above. It follows by a few uncontroversial steps that determinately, the expressions in $A$ are stable across the set of contexts in which the argument is tokened.

Once we have this, the results just sketched kick in. For we have argued that for the material conditional: if extreme inscrutability, then extreme indexical inscrutability. We have also argued that extreme indexical inscrutability would imply that any given argument is not determinately stable in the required sense. But we have already seen that our premises require that it is determinately stable. By modus tollens applied twice, we can infer that extreme inscrutability fails.

Everything turns, therefore, on the first two premises: that some argument is (determinately) in logical good-standing, and that (determinately) good-standing requires stability. It is to the defence of these premises that we turn in the next section.

As with the arguments previously sketched, we consider whether the argument will impact on moderate inscrutability just as much as extreme inscrutability. For definiteness, suppose one were to reject extreme inscrutability, but hold, with Quine, that ‘rabbit’ is indeterminate between a small range of rabbit-candidates (rabbit slices, undetached rabbit parts, etc). Let moderate indexical inscrutability in this setting be the view that it’s indeterminate from one context to the next whether or not the reference of ‘rabbit’ changes from of these candidates to another, or rather stays the same. Can we replace all appeals to ‘extreme indexical inscrutability’ and ‘extreme inscrutability’ in the master argument ‘moderate indexical inscrutability’ and ‘moderate inscrutability’ respectively, and thus get an argument against even moderate inscrutability of reference? If this works for all extant arguments for moderate inscrutability, then we would have reason to reject each such argument.

Much of the argument goes through just as before. But it’s far from clear that we can defend the material conditional: that if moderate inscrutability holds, moderate indexical inscrutability also holds. I see no general reason to think that moderate inscrutability in the absence of extreme inscrutability will generalize in this way. For if we have moderate inscrutability without extreme inscrutability, then the facts that fix meaning must be more extensive than the bare interpretationist allows. We may again take as representative of such a theory Lewis’s insistence that eligibility, as well as fit with sentential data, needs to be optimized by the meaning-giving interpretation of natural language. We are allowed to assume, for present purposes, that rabbit-stages, rabbit-worms and the rest, each lead to equally eligible overall interpretations of the language.
All these interpretations will make ‘Rabbit’ no more indexical than the English expression ‘Rabbit’. The Kaplanian character will be constant: assigning to the predicate the same content no matter what the context is. If Lewis’s eligibility constraint only requires eligible properties to be assigned in each context, then moderate indexical inscrutability may follow. However, I contend that Lewis’s theory should directly assess the eligibility of characters. It is then plausible that the function from contexts to intensions that assigns to ‘Mopsy’ a certain rabbit-stage in one context, a certain four-dimensional entity in the next, and a certain undetached rabbit-part in the third, will thereby be objectively less eligible than a function that assigns to ‘Mopsy’ one and the same rabbit-stage at all contexts. On at least one interpretationist account that denies extreme inscrutability but leaves room for moderate inscrutability, moderate indexical inscrutability will not follow. The moral is more general: those constraints that rule out the ‘extreme’ deviant interpretations may well rule out the kind of radically inconstant interpretations needed for moderate indexical inscrutability. In the nature of the case, it must be determined on a case-by-case basis, whether or not a given account of moderate inscrutability is or is not committed to moderate indexical inscrutability, and thus susceptible to the same criticisms here offered against extreme inscrutability. But unlike the extreme case there is no general argument in the offing against moderate inscrutability.
II

The master argument against extreme inscrutability of reference will go through if we can defend the last remaining premise: the principle that the language involved in logically good token arguments must be (determinately) stable throughout the contexts involved in the argument. My case for this is that we need to endorse the conditional if we are to address a general puzzle about the relevance of logical consequence to token inferences carried out in natural language.

The starting point for the puzzle is the relationship between competent deduction, and the classification of argument types as logically valid or invalid. Competent deductive inference is one of the central ways in which we extend our knowledge, as reflected by the role it plays in formulating central epistemological principles such as closure:

Necessarily, if $S$ knows $p$, competently deduces $q$, and thereby comes to believe $q$, while retaining knowledge of $p$ throughout, then $S$ knows $q$. (Hawthorne, 2004, p.34)

Of course, there are plenty of other constraints on competent deduction beyond simply being logically good. For example, perhaps a competent deducer needs to be aware of the logically good status of the argument he is giving. I take no stance here on the nature and extent of these further conditions that make logically good arguments into competent deductions.

If competent deduction is an epistemically virtuous way of reasoning, how does it earn this status? The natural thought—and the one we will presuppose and explore below—is that it is logically good: good (at least in part) in virtue of being a token of a valid argument-type.

One might try to resist at this point. Competent deductions (arguably) will be modally good (necessarily truth-preserving) and a priori good (a priori truth-preserving) and even a priori modally good (a priori necessarily truth preserving). Might the underlying story about the epistemology of inference allude to this sort of status and simply make no mention of their being tokens of a valid type? To make this more concrete: suppose that we argue that modally or a priori good inferences are good because they are reliable. Perhaps the goodness of arguments of a valid type arises simply because they are reliable: if so, where’s the need to appeal to their specifically logical character?

A full answer to this sort of scepticism about the epistemological significance of logicality is beyond the scope of this essay. But I will mention one important factor. It’s easy to always focus with deployments of good reasoning where we infer $B$ directly by a piece of good reasoning from $A$. Granted that logically good inferences are also good in the more generic respects, one can see why it is appealing to speculate that the full epistemic story may be given at the more generic level. But equally important are cases of indirect arguments, where part of the practice is suppositional reasoning. So, for example, if we can by a piece of (logically) good reasoning get from the supposition that $A$ to $B$, then we are licensed to infer ‘if $A$, $B$’. Many paradigmatic cases of ordinary inferential practice fall into this category: the kinds we describe theoretically as conditional proof, constructive dilemma, reductio, and so forth. Prima facie, part of what we do in evaluating arguments as (logically) good and bad is evaluating whether they are available to be used under the scope of arbitrary suppositions.

It’s not at all clear that the role of logically good inference in suppositional reasoning can be taken over by some more generic sense of good inference. Claiming that we can infer the conditional ‘if $A$, $B$’ on the basis of any generically good argument from $A$ to $B$ is a far stronger than claiming we can infer that conditional on the basis of a logically good argument from one to the other. I think plausible cases can be made that paradigmatic instances of indirect reasoning go wrong if we try to replace appeal to logically good reasoning systematically with good reasoning in some more generic sense. The default position, I suggest, is that logically
good inference is an epistemically important kind. If so, it’d be damaging to any metasemantic theory if it undermined its status.32

6 Validity for indexical languages

It is one thing to point to the feature that separates competent deductions from other forms of virtuous reasoning, and quite another to explain why that feature is epistemically relevant. There is in-principle a gap between the descriptive claim that a competent deduction is of a logically valid type and the normative claim that it is thereby epistemically good.

Tarski famously showed how to make logical consequence formally tractable. He did this by analyzing it via what we now call semantic or model theoretic validity. At a first approximation, something is semantically valid if no matter what interpretation of the non-logical terms we take, the inference is preserves truth from premises to conclusion. So construed, it seems at first glance no mystery that type-validity is a good-making feature of token arguments. It seems that type-validity gives a logical guarantee of reliability; and that seems at least a pro tanto good.

However, the basic Tarskian conception creates a puzzle when we consider indexical language. Repetition is perhaps the most paradigmatically valid inference: yet tokens of this type can fail to be truth-preserving. Consider a move from ‘it is now 12pm precisely’ (said at 12pm) to ‘it is now 12pm precisely’ (said just afterwards). The premise is true, the conclusion false.

The canonical way of extending the definition of semantic validity to cope with indexical languages is given by Kaplan (1979). Validity doesn’t require truth-preservation on an interpretation simpliciter: it requires truth-preservation on an interpretation at each context.33 So while the token argument mentioned above moves from truth to falsity, it does so by exploiting a change in context. The Kaplanian definition rules such cases as irrelevant.34

The strategy of requiring truth-preservation in each context gives a neat classification of the type-validity of arguments in an indexical language. However, defining validity in this Kaplanian way leads to an immediate puzzle about the relevance of the validity of an argument type, so-characterized, to the practice of inferring one thing from another.

In the basic case of a non-indexical, extensional language there is no gap between validity of patterns of inference (inference-types) and the good standing of concrete exemplifications of that type. Since validity guarantees that the inference in question preserves truth simpliciter, the information that inference-pattern I is of a valid type assures us that in any token of type I, the truth of all the premisses ensures the truth of the conclusion.

In the case of indexical languages matters are not so straightforward. If the whole of a token inference occurred in some particular context c, then since a valid inference-type is truth-preserving in every context, it is truth preserving in the one in question. However, token inferences—strings of utterances or inscriptions35—prima facie involve a series of distinct contexts. It takes time to utter or inscribe successively the premisses and conclusion of a token inference. If the premisses and conclusions occur in distinct contexts, there is no guarantee that the token inference will preserve truth, even if it is of a valid type.

We can illustrate this with the reiteration rule. Consider the inference from “Jim walks” (uttered at c1) to “Jim walks” (uttered at c2). The inference-type here instantiated is clearly valid, on Kaplan’s characterization. At any single context, under any re-interpretation, it will preserve truth. However, we can find an interpretation of the vocabulary that will make the premiss true-at-c1 and the conclusion false-at-c2. (Example: Consider the re-interpretation according to which “walks” is an indexical predicate designating walking at c1 and skydiving at c2.) We have an interpretation which makes this combination of inference-type and change of context non-truth preserving. Absent further information, one can conclude nothing about
the truth-preservingness of the actual inference one makes, from the fact that the inference-type
tokened is semantically valid in Kaplan’s sense.

7 The modest proposal

The threat is radical. The validity or otherwise of inference-types threatens to become irrelevant
for the practical purposes of reasoning. Prima facie, all reasoning involves changes of context—
and any such change would seem to render the Kaplanian treatment of validity irrelevant. Our
challenge is to explain the relevance of information about validity of inference-types to the
rightness or wrongness of specific inferential practice.

One reaction is to conclude that we should be interested in some non-semantic notion of
valid inference-type. I think that this would be overhasty. There is a modest solution at hand,
that shows how the semantic validity of inference-patterns can still have practical significance.

The modest idea is the following. We say that a token inference is in logical good standing
if (1) it instantiates a valid pattern in Kaplan’s sense (2) no relevant change of context occurs
during the course of the inference. The contention is that the information that a token infer-
ence’s good standing, in the above sense, guarantees that it preserves truth, and hence will
justify inferential practice. Since part of the characterization of good standing is the validity of
the argument type, we explain why information about validity is relevant to correct inferential
practice.

Note that the characterization of good standing allows irrelevant changes of context to take
place over the course of an inference. Suppose we make an arithmetical inference. Then,
intuitively, no change of context will be relevant to this argument token. Whatever change of
context occurs, the argument will be good.

In formulating things this way, we have as yet given no clear sense to the classification of
token arguments as valid (as opposed to merely instantiating a valid type). I think concentrat-
ing directly on an epistemologically evaluative classification helpfully distances us from some
essentially terminological issues. In my experience, some might feel that practice suggests
that regimentation and disambiguation—in particular, the removal of any worrying context-
sensitivity—is needed before we can classify token arguments as valid or invalid. Some, by
contrast, would like any token argument with true premises and a false conclusion to count as
invalid. I’m not sure much hangs on any of this, but what seems crucial is that we can evaluate
the token inferences we actually perform (not some idealized version of them) as epistemically
proper or not. This is what logical good standing gives us.

Stability, Invariance and Constancy

Which token inferences are classified as good will depend on how we cash out the notion of
‘relevant change of context’. The basic idea here is that a change of context will only be relevant
if it changes the intension of some expression occurring somewhere in the inference. Note that
though condition (1) is, by its nature, appreciable independently of what the particular mean-
ings of the words are, appreciation that (2) obtains will essentially depend on what indexical
character the words have.

Let \( \tilde{C} \) be the set of all contexts involved at some stage of a token inference \( i \). If \( i \) is of a
valid type, then so long as no relevant change of context occurs, we can be sure that we will not
be led from true premises to a false conclusion. To illustrate this, suppose that the \( \tilde{C} = \{c,c'\} \),
and the premises of \( i \) are uttered in \( c \) and the conclusion in \( c' \). Supposing the premises true
is to suppose them true in \( c \), and because \( i \) is of a valid type, this means that the conclusion
is true relative to \( c \). By condition (2), we know that \( c \) and \( c' \) assign the same content to the expressions that feature in the inference (for otherwise, a relevant change of context would have occurred). By compositionality, an assignment of intensions to the primitive parts of a sentence will fix the intension of the sentence as a whole. Hence we know that the conclusion has the same intension when assessed relative to \( c \) and \( c' \). Sentences with the same intension are true in exactly the same situations. Since the conclusion is true in \( c \), it is true in \( c' \) also.

As presented, the argument assumes that all the premisses are uttered in a single context. Clearly the argument will generalize to situations where the premisses are to be evaluated with respect to distinct contexts within an invariant set. Similar considerations will also cover cases where different parts of a single sentence are to be evaluated with respect to distinct contexts.

The basic idea that a change of context will only be relevant if it changes the content of some expression occurring somewhere in the inference needs more exact formulation. I provide two ways of precisifying this notion, formulated for the general case of an intensional, indexical language.

**INVARIANCE** Call a set of contexts \( \tilde{C} \) invariant with respect to a set of expressions \( E \), when each expression in \( E \) is assigned the same intension at every context in \( C \).

**CONSTANCY** Call a set of contexts \( \tilde{C} \) constant with respect to a set of expressions \( E \), if any aspect of context that is used to fix the intension of a term in \( E \) is common to every context in \( \tilde{C} \).

Compare these to the following:

**STABILITY** A set of contexts \( \tilde{C} \) is stable with respect to a set of expressions \( E \), when each expression in \( E \) is assigned the same extension at every context in \( C \).

Notice that constancy entails invariance which entails stability (sameness of aspects of context relevant to determining intension guarantees sameness of intension, which guarantees sameness of extension). Of course, the stability, in this sense, of the expressions and contexts in play in token argument \( A \) is just what is expressed by \( \text{STAB}(A) \).

Either invariance or constancy could be used as an explication of condition (2), but either way, a good argument has to be such that the relevant set of contexts is stable with respect to the expressions involved, precisely in the sense relevant to the truth of the conditional needed to complete the master argument against extreme inscrutability.⁴⁶

### 8 Objections and responses

**Objection 1.**

Constancy is too demanding to play the role envisaged above. For context is constantly changing: utterances of premisses and conclusions are never totally simultaneous, for example. No inference involving any temporal indexical will ever correspond to a constant set of contexts.

**Reply 1.**

One could, of course, shift to invariance as an explication of stability, rather than constancy. But a less concessive response is available: one can question whether the context change involved in the above inference does render the set of contexts inconstant. On one view, contexts comprise a string of factors: the time, place, agent, world, etc. at which
the utterance takes place. On this picture, the character of the indexical “Today” would be something like “the day containing the temporal component of context c”. There is then a relevant difference in context during the above inference; and hence the set of contexts associated with the inference would be inconstant. The current objection tacitly presupposes this kind of setup.

An alternative is to represent contexts as centred worlds, and appeal to auxiliary functions that pick out aspects of those worlds. For example, the interpretation of ‘today’ would be given by ‘\( \text{DAY}(c) \)’. The ‘aspect’ of the context that is required to be invariant in the case of the “Today” inference, would be \( \text{DAY}(x) \) for \( x \in \mathcal{C} \). This kind of setup is attractive, if only because it seems hopeless to list once-and-for-all all the possible aspects of context that could be relevant to determining the reference of an indexical expression.\(^{37}\)

If this is the case, then one can analyze goodness in terms of constancy, while still classing the ‘Today’ inference as good.

Objection 2.
The account fails to capture the interesting logical or conceptual connections between indexical utterances uttered in different contexts. From ‘it is the case that \( F \)’ we can legitimately infer, at a later point, ‘it was the case that \( F \)’. This inference is not valid in Kaplan’s sense, and so the token will not be in good standing, in the current sense.

Likewise, the account fails to cover some obviously valid patterns of inference. For example, consider the inference from ‘it is now 13.46.24 precisely’ to ‘everything is self identical’. The argument is clearly a good one, in virtue of the consequent being a logical truth, but since the temporal component involved in the antecedent will alter through the course of the inference, it will not be ‘good’ in the sense sketched above.

In the light of these issues, is it really plausible that the Kaplanian characterization, supplemented by the modest proposal, gives us the right handle on logically good inference?

Reply 2.
If we had some rival account of logically good inference compatible with extreme indexical inscrutability then these challenges would be serious. The observations here are by no means knock-down objections to the account given here, which at least gets the paradigmatic cases right.

As it happens, I think the account can be naturally extended to take account of these phenomena. On the first point, I think (but will not defend here) that ‘dynamic inferences’ such as these can be accommodated within the setting given here, if we have the right theory of indexical expressions.\(^{38}\)

On the second point, grant pro tem that the inference is not logically good, in the relevant sense. What bad results follow? Notice that we can characterize a derivative sense in which the inference is well-made. For example, the inference from the null set of premisses to ‘everything is self identical’ is valid. If we know this, and also know that (quite generally) a token argument will never take us from truth to falsity if it is a weakening of one that is in good standing, then we know enough to explain how we appreciate the truth-preservingness of the original argument. I anticipate telling similar stories, on a case-by-case basis, for other examples adduced.

Objection 3.
We need not think of token inferences as involving change of context at all. The modest proposal is therefore unnecessary: semantic validity will suffice.
Reply 3.

This is a view suggested by Williamson (1997). After describing the Kaplanian treatment of validity for indexical languages, Williamson notes the challenge:

There is a problem. On this account, the validity of an argument tells us nothing about truth-preservation when the premises and conclusion are instantiated in different contexts. However, inference takes time: we judge the premises and conclusion successively. Thus the account of validity looks irrelevant to the inferences we actually make. (Williamson, 1997, p.652)

Williamson holds that the problem only arises if we focus on the relations between occurrent judgements. Plausibly, it takes time to move from judging (or supposing) that premises hold, to judging that the conclusion follows. However, Williamson contends that we should properly be focusing on belief states, which can be retained over time. These simultaneous belief states can be considered as instantiating, or failing to instantiate, a valid pattern of inference; and no concern about the involvement of different contexts emerge.

I think two points show Williamson’s approach does not get the heart of the issue. Let us suppose pro tem that his suggestion handles cross-temporal context change. Nevertheless, there are other aspects of context that may still vary between premises and conclusion of an inference. We can bring this out with a simple, though admittedly artificial, indexical expression. Let me introduce the indexical ‘blig’, which will refer to the primary connective of any sentence or sentence-like structure in which it figures, and to the Taj Mahal otherwise. ‘Blig is the Taj Mahal’ is true; but ‘Blig is the Taj Mahal and Blig is the Taj Mahal’ is false.

The point is the placement of the indexical itself is potentially an aspect of the context with respect to which the indexical is assigned a referent. Though the example is artificial, it would be most uncomfortable to exclude expressions with this feature a priori. Indeed, more standard philosophical examples might well be analyzed as involving expressions of this type: e.g. self-referential sentences or thoughts such as “this very sentence is short”, which presumably rely on aspects of context such as the demonstrated sentence. A related point is that context can change within a sentence (Lewis, 1979, p.241). If the above proposals are accepted, we look in danger of developing a notion of context and inference that is unable to discharge its other theoretical roles. We need to accommodate such context change, not eliminate it.

Further, the account stands in need of an extension to handle ascriptions of validity to sequences of occurrent judgements, written and spoken inferences, and the like. We do evaluate such sequences of events as valid or invalid, and we need a reconstruction of this practice. Since the issue of cross-context inferences has not been taken head-on by the Williamson proposal, we have no ready-made proposal for such cases. Presumably, such ascriptions of validity must be handled derivatively from the primary notion of a valid inference involving belief states—but we have been given little indication how this is to be effected.

Objection 4.

There is an obvious response that the current discussion misses. We should distinguish the context in which a judgement (or utterance) is made from the context with respect to which a judgement (or utterance) should be assessed. Accordingly, we should think of a token inference as assessed at for a single context—though it is indeterminate which
one this should be. Since semantic validity guarantees truth-preservation in all contexts, it guarantees truth-preservation no matter which of these contexts we take to be the actual one.

Reply 4.
This strategy is canvassed by both Campbell (1997) and Williamson (op cit). However, it is easy to find examples where it delivers inappropriate results. Consider an argument of the following form:

This very second is an even number of seconds after $t$

This very second is an even number of seconds after $t$

Now, if some time has elapsed between the judgement that the premiss holds and the drawing of the conclusion, it is clear that the ‘argument’ by reiteration should not be taken to be in good standing. However, every choice of context will declare it valid, since a choice of context will determinate a time which will be the referent of ‘now’ in each case. Assessing the token argument with respect to a single context delivers exactly the wrong result: this is an instantiation of a valid argument type that we want to come out invalid.

The point becomes more dramatic if we use the indexical ‘blig’, introduced above. Consider the following argument:

Blig is the Taj Mahal

so:

Blig is the Taj Mahal and Blig is the Taj Mahal

The premise is unambiguously true (in a sentence with no main connective, ‘blig’ will designate the Taj Mahal); the conclusion is unambiguously false (in a conjunctive sentence, ‘blig’ will designate Conjunction). With respect to any single choice of context, ‘blig’ will have to designate a single object; and hence the argument will come out as truth preserving. Again, the argument-type is truth preserving, but no argument token should be described as in good standing.

The point is that the separate elements of the token argument—the token premiss and conclusion—call for distinct contexts. We cannot force them into a single context without clear distortion of the intended use of the expressions. There just is no admissible single context for the token inference.

We were looking for conditions that articulate what it is for a token argument to be in logical good standing. Being a token of a valid type is not sufficient. I have argued that the modest proposal resolves our puzzle here. It does not lead to unacceptable consequences (pace the objections above); and moreover, the rival suggestions proposed by Williamson and Campbell fail.

The modest proposal neatly resolves a puzzle about the epistemic relevance of type-validity. But in the present context it has a wider significance. For, by requiring that expressions in token arguments be constant or invariant through the contexts in play, it requires a fortiori that they be stable, in the sense that their extensions remain the same throughout those contexts. Determinately, if $A$ is a logically good token argument, then it is stable.
Extreme inscrutability is counterintuitive. But it is a consequence of an otherwise attractive theory of linguistic content: an elegant form of interpretationism. That motivates the project of weighing the benefits and costs of this metasemantic package.

Flat footed appeals to intuitions are dialectically weak, teach us little, and such intuitions may in any case be ‘explained away’. But it turns out to be surprisingly difficult to pin down precise theoretical costs that the inscrutabilist faces. I argued in the first half of the paper that there are prima facie lines of resistance to the central lines of argument one might try against inscrutabilism.

The master argument of this paper, however, gains traction against the inscrutabilist. It shows that there is a tension between extreme inscrutability (adopting on the basis of permutation-style arguments) and the epistemology of inference. There are two key premises to the master argument. The first is that extreme inscrutability generalizes to extreme indexical inscrutability. This is not immediate (in particular, there is no logical entailment from the former to the latter). But we can argue for the truth of the needed material conditional. The argument was sketched in the text, and is developed in formal detail in the appendix. Importantly, there is no general reason to think the analogous conditional holds when it is moderate rather than extreme inscrutability that is at issue.

The other key premise is that, determinately, token arguments which are ‘logically good’ involve no change of extension across the contexts they cover. The second half of the paper argues that, in order to resolve a puzzle over the epistemic relevance of (type) validity, we need to analyze ‘logically good’ in a way that secures this conditional.

The master argument shows that from the determinate logical good standing of any token argument, one can deduce the falsity of extreme inscrutability. Accordingly, the price of inscrutability is that no token argument is determinately in logical good standing. One might be willing to pay much to secure a workable reductive theory of linguistic representation: but the price that (extreme) inscrutability extracts is too high.
Appendices

In the following appendices I provide the formal overgeneration results referred to in the main text. I show that these results hold in the kind of setting used by many linguists to provide a semantic theory for natural language: the generalized semantics of Lewis (1970). In appendix A I develop the tradition permutation arguments in this highly general setting. In appendix B I show how to prove the extreme indexical inscrutability result at the heart of the criticisms of inscrutabilism developed in this paper.

A Permutation arguments preserving truth-conditions

In some interpretationist settings, one’s data consist of a pairing of sentences with coarse-grained propositions or intensions (cf. the interpretationism described in Lewis (1975)). The target is to preserve, not only the truth-values of certain sentences, but the truth-conditions of sentences. In the current setting we shall think of truth-conditions as given by sets of possible worlds, or characteristic functions of such sets: this tells us the worlds in which the sentence is true. Of course, if we can show that permuted reference schemes assign the same truth-conditions to sentences, then it will follow immediately that they assign the same truth value at the actual world to sentences.39

We will show how arbitrary permutations of the extension of singular terms can be embedded within an overall interpretation which leaves the truth-conditions assigned to sentences invariant. In fact, the setting is more general. The semantics will assign to sentences functions from indices to truth-values, where the indices specify not only a possible world, but also a time, place, and other factors. If we can show that the permuted variants of an interpretation leave the semantic value of sentences invariant, we shall have what we need.

We first prove the result for the general semantic setting of Lewis (1970) (what Cresswell (1973) calls a ‘pure categorial language’). We first set out the framework itself, and then state and prove a permutation theorem for the setting. We shall then describe how the framework is altered to take into account indexicality, and extend the permutation argument to that ‘double-indexed’ setting.

The framework (syntax): a pure categorial language

The framework in which we operate initially is a general semantics, in the sense of Lewis (1970). The atomic expressions of the language will be given by a lexicon, and there will be phrase-structural rules saying how admissible compounds can be built up from elements of the lexicon. The lexicon and the phrase-structural rules give the analogue of a definition of well-formedness within a formal language.

The framework that Lewis recommends is drawn from Ajdukiewicz’s (1935) categorial grammar, and is what Cresswell (1973) calls a ‘pure categorial language’ (essentially, this is a form of type theory, without any ‘syncategorematic’ terms such as λ-operators). In the lexicon, atomic expressions will be associated with categories, and then the well-formedness of compounds will be determined by whether the categories of the components dovetail. For example, the category of the lexical item “Susan” might be that of ‘names’ (N), and the category of the lexical item “runs” might be ‘intransitive verb’ (S/N)—the notation reflecting the fact they when combined with a category N expression it produces a category S expression (a sentence).

The categories themselves are characterized recursively. N and S are ‘basic categories’40 Given categories c,c₁,\ldots,cₙ, we have a derived category c/c₁,\ldots,cₙ. In the above, ‘runs’ is in
the derived category $S/N$. Writing “+” for concatenation, the general rule of well-formedness is that for any expressions $e, e_1, \ldots, e_n$, we have $e + e_1 + \ldots + e_n$ well-formed iff $e$ is of a derived category $C/C_1, \ldots, C_n$ and each $e_i$ is of category $C_i$. “runs(Susan)” is well-formed because it is of the form $(S/N) + N$, and so fits our template.\(^{41}\)

Notice that the complexity of the category of an expression and its syntactic complexity cross-cut. Basic lexical items—the atomic expressions—will typically have quite complex categories: for example, the atomic adverb ‘fast’ will have category $(S/N)/(S/N)$ (it yields a verb phrase when a verb phrase is input). Conversely, expressions of the basic category $S$ (sentences) will be syntactically complex.

The result of such concatenation won’t look much like English. A very basic example is that ‘Jill loves Jane’ would be represented by the word-order ‘(loves(Jane))Jill’ within the system just developed. Additional work is required to explain how such analyses relate to natural language. What we need here is some kind of mapping from our ‘disambiguated’ formal language to ordinary sentences of English. This ‘ambiguating relation’ may take one of a number of forms, depending on what other resources from linguistics one wishes to bring to bear. Lewis (1970, p.204) appeals to a transformational component of the grammar; Dowty (1979) suggests various ways to integrate the setting with generative semantics.\(^{42}\)

The framework (semantics): single-indexed general semantics

What we have so far seen is a treatment of the syntax of a formal language. We now describe the Lewisian “general semantics” which will associate each well-formed expression with a semantic value. The kind of semantic value for a given expression will be what Lewis calls an “appropriate intension”—which intensions are appropriate being determined recursively by the category of the given expression. The base cases are handled individually. For sentences (expressions of category $S$) an appropriate intension will be a function from indices to truth-values. For expressions of category $N$, it will be a function from indices to objects.\(^{43}\) Appropriate intensions of derived categories are then functions between intensions appropriate to the categories from which they are derived. For example, expressions in category $S/N$ will be assigned functions from intensions appropriate to category $N$ expressions to intensions appropriate to category $S$.

We can capture this by characterizing intensions in terms of their type. Let indices be of type $i$, objects type $o$ and truth-values type $t$.\(^{44}\) Let the type $\langle a, b \rangle$ include all functions from elements of type $b$ to elements of type $a$. We can then formulate the above by saying that an appropriate intension for category $S$ is a function of type $\langle t, i \rangle$; an appropriate intension for the category $N$ is of type $\langle o, i \rangle$; and in general the appropriate intension for category $c/d$, where $c$ is of type $\alpha$ and $d$ is of type $\beta$, will be of type $\langle \alpha, \beta \rangle$.\(^{45,46}\)

A lexical interpretation $||$ will be an assignment of semantic values to basic parts of the language—the elements of the lexicon (e.g. names, adjectives, verbs, adverbs etc). We now have the idea of a lexical interpretation function for a categorial language, and a characterization of the type of semantic value appropriate to complex expressions. We need to ‘extend’ the lexical interpretation function to give an overall assignment of semantic values to arbitrary well-formed expressions in the language.

We let a model $m$ for the language include a domain $U$, a set of indices $I$, and a lexical interpretation function $||$. Then one could let a model induce a valuation $v_m$ for arbitrary well formed expressions:

1. For $e$ in the lexicon, $v_m(e) = |e|$
2. For $e' = e(e_1, \ldots, e_n)$, $v_m(e') = v_m(e)[v_m(e_1), \ldots, v_m(e_n)]$
In what follows, I will choose a slightly different, though equivalent, setting. I will speak of an arbitrary valuation || as any function taking expressions to intensions appropriate to their category. Such valuations may very well be totally crazy: what we typically do is to restrict attention to the well-behaved ones. I say that || embeds a lexical interpretation scheme if that scheme coincides with the restriction of || to lexical elements. I call a valuation || compositional if the following general relation holds:

\[ |e(e_1, \ldots, e_n)| = |e|[|e_1|, \ldots, |e_n]| \]

We then let models contain compositional valuations, rather than lexical interpretation schemes.\(^47\)

This finishes the description of the syntax and semantics of our ‘single indexed pure categorial language’. To summarize:

1. Our language consists of infinitely many categories of expressions, described via a categorial grammar. \(S\) and \(N\) are basic categories. If \(C\) and \(C_1, \ldots, C_n\) are categories (basic or derived), let \(C/C_1 \ldots C_n\) be a derived category.

2. We have a set of indices, \(I\) and a domain of objects \(O\), a set of truth-values \(\{T, F\}\), and a valuation ||.

3. The valuation || assigns intensions to each expression appropriate to its category. Appropriate intensions for each category are functions whose type reflects the build up of the category, in the fashion described above.

4. Call a valuation compositional iff the semantic projection rule of function-application is met. Suppose we have an expression \(e\) of category \(C/C_1 \ldots C_n\), and expressions \(e_i\) of categories \(C_i\) (so that the complex expression \(e(e_1 \ldots e_n)\) will be of category \(C\). Then it must be that:

\[ |e(e_1 \ldots e_n)| = |e|[|e_1|, \ldots, |e_n|] \]

**The permutation argument within single-indexed general semantics**

Let us introduce two further notions. First, call two compositional interpretations sententially equivalent if they assign the same intensions to everything of category \(S\). Second, say that a valuation embeds the reference scheme \(r\) (relative to index \(i\)) iff whenever \(e\) is of category \(N\), \(|e|(i) = r(e)\). The aim now is to show that we can always construct sententially equivalent compositional valuations which embed arbitrarily permuted reference schemes.

The theorem we will prove shows that any coherent\(^48\) assignment of semantic values (i.e. appropriate intensions) to sentences can be made compatible with arbitrarily permuted reference schemes. We do this by defining the notion of a \(\phi\)-variant of a valuation, where \(\phi\) is a permutation of the domain of objects. If || is a valuation embedding at index \(i\) the reference scheme \(r\) that, e.g. assigns Susan to “Susan”; then the \(\phi\)-variant ||\(\phi\) of || will embed at \(c\) a reference-scheme \(r_\phi\) that assigns \(\phi(Susan)\) to “Susan”. Rather than setting up a permuted lexical interpretation scheme and proving by induction that the valuations determined by the original and \(\phi\)-variants appropriately match, I shall define directly the \(\phi\)-variant valuations, in a way that makes obvious the fact that they are sententially equivalent to the valuation from which one starts, and that they embed an appropriate permuted reference scheme. The challenge will then be to show that the definition is legitimate: i.e. that the permuted valuation, so-defined, is compositional. We must show that the semantic values that it assigns to complex expressions arise in the appropriate way from the semantic values it assigns to the lexical basis.

The construction of the \(\phi\)-variant valuations is as follows:
Let \( \phi \) be an arbitrary permutation of \( O \). Define recursively the \( \phi \)-image of an intension as follows:\(^{49}\)

- If \( f \) is an appropriate intension for \( S \), then \( f^\phi = f \)
- If \( f \) is an appropriate intension for \( N \), then \( f^\phi = \phi \circ f \)
- If \( f \) is an appropriate intension for \( C/C_1 \ldots C_n \),
  then \( f^\phi : r^\phi \mapsto g^\phi \iff f : r \mapsto s \).

Given a valuation ||, let the \( \phi \)-permuted valuation ||\( \phi \) assign to \( e \) its \( \phi \)-image; i.e. for each \( e \), \( |e|_\phi := f^\phi \) where \( f = |e| \).

Notice that, by construction, a \( \phi \)-variant of a valuation \( v \) will embed a reference scheme that is permuted by \( \phi \). Moreover, a valuation and its \( \phi \)-variant will be sententially equivalent, again by construction. What remains to be shown is that the \( \phi \)-variant is a legitimate valuation of the language—that is, that it is compositional in the sense delimited above. That isn’t hard:

**Theorem 1.** For any permutation \( \phi \), ||\( \phi \) is compositional if || is.

**Proof.** Suppose || is compositional. Take an expression \( e \) of category \( C/C_1 \ldots C_n \), and expressions \( e_1 \ldots e_n \) of categories \( C_1 \ldots C_n \) respectively. The complex expression \( e(e_1 \ldots e_n) \) will be of category \( C \). By compositionality of ||, we have:

\[
|e(e_1 \ldots e_n)| = |e|(|e_1|, \ldots, |e_n|)
\]

We need to show that:

\[
|e(e_1 \ldots e_n)|_\phi = |e|_\phi(|e_1|_\phi, \ldots, |e_n|_\phi)
\]

We show this for the case \( n = 1 \), the other cases being trivial extensions. Write \( e_1 = d \). From the compositionality of || we have: \( |e(d)| = |e|(|d|) \); i.e. \( |e| : |d| \mapsto |e(d)| \). By the definition of the \( \phi \)-image this gives us: \( |e|^\phi : |d|^\phi \mapsto |e(d)|^\phi \). Given the way that ||\( \phi \) is defined, we can rewrite this as: \( |e|_\phi : |d|_\phi \mapsto |e(d)|_\phi \), i.e.:

\[
|e(d)|_\phi = |e|_\phi(|d|_\phi)
\]

so compositionality is secured.

The permutation argument within double-indexed general semantics

Indexical expressions are commonly thought to require the semantic values we have been discussing to be changeable: an expression may express different such values when uttered in different contexts. One option within a general semantics is to include context (represented as a ‘centred world’) as one index within the above account.\(^{50}\) Within that setting, our proof runs just as before.

Alternatively, one can separate world, time, delineations etc. from context, to “double index” the general semantics.\(^{51}\) Syntactically, everything is unchanged. Within the semantics, however, expressions are assigned characters rather than intensions, where a character is a function that maps contexts to Lewisian compositional intensions. We need the notion of an ‘appropriate’ character for a given category of expression. Therefore, say that a character is of type \( \tau \) iff it maps contexts to intensions of type \( \tau \); and wherever the appropriate intension for category \( c \) was type \( \tau \), appropriate characters will be those of the same type.

Formally, characters resemble ‘Carnapian intensions’ rather than the ‘compositional intensions’ of Lewis’ general semantics. Consider, for example, an intransitive verb (category \( S/N \)).
In Lewis’ general semantics, its semantic value was the function from semantic values of type $N$ to semantic values of type $S$. On the double-indexed proposal, by contrast, its semantic value is a function from contexts to intensions; i.e. the context index is treated in a ‘Carnapian’ way. The upshot of this is that the semantic projection rule cannot simply be function-application, as within the original Lewis treatment. We can still have a single rule appropriate to arbitrary concatenations, however. Consider an expression $a(b)$, where $b$ is of category $c_1$ and $a$ is of category $c_2/c_1$. If $a$ has character $A$ and $b$ has character $B$, then the character of $a(b)$ maps context $\alpha$ to the intension that results from “compositionally” applying $A(\alpha)$ to $B(\alpha)$.

We need to spell out what the permuted interpretation function is for this new setting. This is defined in the obvious way. If $|e|$ is $\sigma$, where $\sigma : c \leftrightarrow g$, then $|e|_{\phi}$ is $\sigma^\phi$, where $\sigma^\phi : c \leftrightarrow g^\phi$, where $g^\phi$ is the $\phi$-image of the intension $g$. Notice that since $g^\phi = g$ when $e$ is a sentence we have that $|e|_{\phi} = |e|$ for $e$ a sentence. The permuted interpretation not only holds the intensions of sentences invariant, it holds the characters invariant also.

**Derivative invariance results**

We have seen that we can leave the semantic values of sentences invariant under permutations of the reference-scheme in a rich class of settings. The ultimate aim of such results is to argue for extreme inscrutability, by saying that all such ‘sententially equivalent’ semantic theories are equally good at fitting the data which the interpretationist provides. Such data may not take the form of a pairing of sentences with something as rich as the compositional intensions or characters that we have just been looking. It might rather involve a pairing between sentences and propositions—the set of circumstances in which the sentence is to be true.

In such a setting, what we need for our purpose is that semantic theories that differ by containing permuted reference-schemes can assign to sentences the same truth-conditions (function from possible worlds to truth-values). This follows immediately from the above result once we note that the truth-conditions of a sentence are determined by the semantic value of that sentence in the rich settings just canvassed. If semantic theories are sententially equivalent, then they will assign to sentences the same truth-conditions.

To illustrate this, let us show how to construct two senses of ‘truth-conditions’ for a sentence $S$. These are what are known within ‘two-dimensional modal logic’ as the $C$-intension and the $A$-intension of a sentence.

For $w$ a centred world (i.e. a context), define the matching-relation $m(x,y)$ to hold between world $w$ and string of indices $i$ iff the world, time etc. components of $i$ match those given by $w$. First, we will define the $C$-intension of a sentence $s$ at a context $c$. This is a set of centred worlds given by:

$$w \in C(s) \iff \forall i(m(w,i) \rightarrow (|s|(c) : i \mapsto T))$$

Second, we will define the $A$-intension of a sentence. This is the set of centred worlds given by:

$$w \in A(s) \iff \forall i(m(w,i) \rightarrow (|s|(w) : i \mapsto T))$$

To see the difference between these two constructs, consider the sentence “he is Beckham”, uttered while pointing at the famous footballer. The $C$-intension is the set of worlds where the person indicated (i.e. Beckham himself) is identical to Beckham. On standard assumptions, then, this is the necessary proposition—the set of all possible worlds. The $A$-intension is the set of worlds where the person indicated by the pointing is Beckham. It is false, therefore, with respect to possible worlds where Beckham stayed at home and sent out his double to make the public appearance. Notice that the $A$-intension is contingent where the $C$-intension is necessary. It is arguable, in the light of these distinctions, that the data for a semantic theory might be given
in the form of a pairing of sentences with A-intensions. It is reassuring for the inscrutabilist, then, that all these sentential constructions are invariant under the permuted valuations. This can be easily checked by noting that the only appeal to the valuation || in the above definitions is in application to sentences, where, as we have seen, || and ||φ coincide.

B Indexical-inscrutability: a cut-and-shunt argument

We have examined arguments focused on what might loosely by termed “synchronic” inscrutability of reference. We now prove a “diachronic” version. An expression such as “London” will, on the standard interpretation, designate London no matter what the context is. Likewise, the deviant interpretations assign to that term a single object—Sydney, say—at all contexts. Because the reference of a term is at all times the image under the permutation of its original reference, the pattern of indexical dependence of reference will be the same on each of the permuted interpretation schemes.

We now have the resources to extend the arguments so that they imply a kind of ‘indexical inscrutability’. The extreme indexical inscrutability thesis is that, if c and c′ are distinct contexts, then there is no fact of the matter whether e designates the same object at c as at c′. To get this result, we ‘cut-and-shunt’ some of the permuted interpretations constructed above. The intuitive case is straightforward. By the results of §2, we have two valuations that always agree with each other on the content assigned to whole sentences, no matter what context is chosen. If we construct a third valuation, which matches valuation-1 at some contexts, and valuation-2 at the remainder, it will also have this property—all three will agree on the content of sentences at each context. Our first valuation might have it that ‘London’ denotes London at all contexts, whereas our second valuation has it that it denotes Paris at all contexts. The constructed valuation will agree with the first on some contexts, with the second on others—so it depicts ‘London’ as indexical. Yet it is sententially equivalent to the originals, and so under the current assumptions, the interpretationist has no grounds for ruling it out. What we do below is sketch how this intuitive idea could be formalized within the double-indexed semantic setting given above.

Take the candidate double-indexed valuation, ||2. Relative to a given context c, the designated valuation determines what would be a valuation within the single-indexed semantics, i.e. an assignment of compositional intensions to expressions:

\[ |e|^{(1,c)} := |e|^2(c) \]

We have seen how to construct sententially equivalent φ-variant interpretations ||φ of a arbitrary single-indexed valuation || in the proof of the permutation result for the single-indexed case, and we can apply these techniques here, yielding the φ-variants ||φ\((1,c)\).

Now assign permutations φi to contexts via a function P. Relative to P, we construct a new double-indexed valuation, which we call the P-variant of ||2 and denote ||P2.

Given an expression e and a context c, we let ||P2 assign to an expression e the intension given by ||φ\((1,c)\) at e, where \( φ = P(c) \), i.e.:

\[ |e|^2_{P}(c) = f \iff |e|^{(1,c)}_{φ} = f \]

We now argue that ||P2 is sententially equivalent to ||2. At any given context c, the intension assigned to a term is that assigned to it on some ||φ\((1,c)\). However, the intension assigned by ||φ\((1,c)\)
to a sentence is exactly that assigned to it by $|^{(1,c)}$, by our previous results. By construction $|^{(1,c)} = |^2(c)$, so for all contexts $c$, $|^2(c) = |^2_P(c)$. QED.

By choosing $P$ appropriately, we get extreme indexical overgeneration. Consider “London”, which we shall suppose to be of category $N$. Given contexts $c$ and $c'$ pick $P$ where $P(c)(London)=London$ and $P(c')(London)=Paris$. Then on the $P$-variant interpretation, “London” will pick out London as uttered at $c$ and Paris as uttered at $c'$. Since the variant interpretation is sententially equivalent to the original interpretation, given BEST=FIT, it is not determinately incorrect.

Equally, by choosing the contexts and permutations carefully, we could take an indexical expression and give it a constant reference. One could choose $P$ so that the permutation $\phi$ appropriate to a given context $c$ maps the speaker of that context to London. Relative to that valuation, ‘I’ is a non-indexical expression referring to London irrespective of context. Again, by the argument above, such interpretations are not determinately excluded.
Notes

1My working assumption is that a type theoretic, multiply intensional semantics of the form described by Lewis (1970) suffices to interpret natural language. For discussion of how permutation arguments look within Davidsonian semantic theory, see Williams (2008).

2Of course, the correlation may not be perfect: sometimes people speak falsely! Different theorists deal with imperfections in the correlation in different ways. It is the basis for the famous defense of the ‘principle of charity’ in Davidson (1973): the default assumption must be that people speak truly. Lewis (1975) takes a different approach, with the relevant correlation being between the states of the world that speakers believe to obtain, and the sentences they utter.

The approach just described contrasts sharply with what Davidson (1977) calls the ‘building block’ approach where one’s philosophy of linguistic representation gives priority to sub-sentential reference. A locus classicus here is Field (1972).

3A variation would be to look at patterns of assent and dissent among ideal speakers. This is the form discussed in Putnam (1980).

4Lewis in later work complicates this picture by putting extra constraints on successful semantic theory. I discuss this briefly below.

5Versions of the permutation argument are given in Jeffrey (1964); Quine (1964); Field (1975); Wallace (1977); Putnam (1978); Davidson (1979); Putnam (1981). The most detailed presentation of the results that I know of is in the appendix to Hale and Wright (1997).

6That in the appendix to Hale and Wright (1997).

7Thanks here to Matti Eklund and a referee for this journal, for urging me to consider the applicability of my considerations to moderate inscrutability theses.

8These, and other objections, are discussed in more detailed in my Williams (2005, ch 6.)

9For the view that understanding is knowledge of meaning, see Dummett (1976). For the view that it at least consists in beliefs about meaning, see Heck (2005). For the view it consists in some other kind of attitude, see Garcia-Carpintero (2000); Stanley (2002).

10One might find tension if competence consisted in knowing the meaning of sentences alone, where ‘meaning’ is richer than simply Lewisian ‘truth-conditions’; for example, if it consists in knowing what structured proposition the sentence expresses, as canvassed by Soames (1989). I will not discuss this here, however.

11To emphasize, McGee’s arguments were originally intended to show that the permutation arguments themselves do not go through. But I think they are better seen in the current light. To anticipate, his arguments that permutation arguments fail require us to build it in to the semantic setting we choose, that e.g. the extension of something at a world must be exist at that world; or that certain expressions cannot be but rigid (the strongest case for the latter being in the case of variables, which in most possible worlds semantics are treated as automatically rigid). As shown in the appendix, there’s no formal reason for the inscrutabilist to accept such settings.
(including the putative rigidity of variables). It seems better, therefore, to present the case as one
where we are invited to consider such features costs that the inscrutabilist incurs

12 I give detailed consideration to each of the above in my Williams (2005, ch 6.)

13 For examples of this tactic, see McGee and McLaughlin (1994) on ‘pluth’, and the view
ascribed to Hartry Field in Loewer (2005) and McGee (2005b).

14 Talking of different ‘interpretation functions’ is, of course, just to talk about certain math-
ematical objects, functions from words to objects.

15 Compare Hale and Wright (1997).

16 Consider, for example, Williamson (2000), who thinks that at worlds where I was never
born, I nevertheless exist as an abstractum. On a Williamsonian view, the most we can get out
of McGee-style considerations is that it is indeterminate whether or not we are referring, at a
world, to things that are concrete at that world. That result lacks the shock value of the original
thesis.

17 The rigidity of variables is even more deeply embedded, but I am not aware of any argu-
ments for this thesis, so I’m taking it that the simple availability of workable systems where
variables are non-rigid, as sketched in the appendixes, suffices here.

18 This, of course, is not meant to be a criticism of Kripke’s arguments: his main target was
the kind of non-rigidity that descriptivists postulated; in that dialectical context, he was entitled
to ignore possible extreme inscrutability.

19 A striking disanalogy between the temporal and modal cases is that we are causally con-
nected to (say) Beethoven, whereas we are not causally connected to mere possibilia. But for
this disanalogy to have relevance, we must explain why causal contact is a precondition on re-
ferring. This would be straightforward on, say, a metasemantics that proposes to identify the
reference relation with certain causal relations. But the inscrutabilist is working within a set-
ing where the metasemantics is not causally constrained in this way (otherwise the argument
for extreme inscrutability couldn’t even get started). So again, it’s not clear what the argument
against the inscrutabilist is supposed to be.

20 The case is very different from that of empty names: empty names are those that fail to
secure a referent. What is under consideration here is a case where reference is secured to
something that fails to (actually) exist.

21 In the literature on supervaluationist vagueness, analogous coordinations are used to ex-
plain so-called ‘penumbral connections’: $A \land \neg A$ can be determinately false, even if $A$ and $\neg A$
are each indeterminate.

The fallacious move is of the following form: from $\neg Dp, \neg Dq$; move to $\neg D(p \land q)$. This is
directly comparable to the fallacious move within modal logic (which likewise has some initial
appeal): moving from $\Diamond p, \Diamond q$ to $\Diamond(p \land q)$.

22 In an appendix to this paper, I give the formal details.

23 This sketch of the extreme indexical inscrutability result is proved in formal detail for rich
languages in the appendix to this paper.
Our argument for this is that the canonical arguments for extreme inscrutability generalize to establish the strong result. We are not in a position to argue for the stronger claim that indexical inscrutability itself necessitates extreme indexical inscrutability. The defence of the material conditional is the following. Either the arguments work or they do not. If they work, they establish both results, and so the material conditional is true. If they fail, then we have no extant reason to believe that extreme inscrutability holds—and given its radical nature, we have every reason to believe that it fails. But that would again make the material conditional true.

The independent case for this turns on the correct interpretationist response to scenarios such as Strawson’s ‘massive reduplication’ worlds (Strawson, 1959, ch.1). I briefly discuss these in Williams (2007). See Hawthorne (2007) for some critical discussion of the ‘eligible characters’ proposal.

I do not mean to use ‘logical consequence’ in an overly narrow manner, however. I am quite amenable to thinking that ‘analytical’ inferences (say, from ‘M is red’ to ‘M is coloured’) are in the relevant sense valid, though they are clearly not valid in the narrowly logical sense. The semantic treatment of validity is easily extendable to such cases.

Hawthorne (op cit) makes a number of sensible further points. Competent deduction may require more than inferring in a way that accords with a valid form: it might require that we be aware of this fact, or have followed a proof. I have no quarrel with this at all: indeed, my claim here is, in effect, that the stability of the language involved must form one part of competent deduction.

Hawthorne further claims: “a competent deduction need not consist of a formally valid argument” (p.35). I take it that by this he means that there is no reason to restrict closure to cases of narrowly logical deduction. But in saying this he in no ways denies that narrow logical deduction is one of the central and important cases where closure holds. Further, I contend that competent deduction in general always involves arguments of types which are semantically valid in a broad sense: for semantic characterization of validity only coincides with narrowly logical validity on one particular choice of what to hold invariant across reinterpretations. If we allow ‘meaning postulates’ to constrain legitimate reinterpretations, then the cases Hawthorne mentions: e.g. ‘that is red’ to ‘that is coloured’ will indeed be semantically valid. But this broad notion of validity, again applying in the first instance to inference-types, raises exactly the same issues as the narrow notion.

this isn’t uncontroversial: for example, Kaplan (1989) argues that ‘I am here now’ is a logical validity, but not necessary; so it’d be logically good but not modally good.

Though again, this will be controversial: it may be that epistemology of a priori or modally good inference proceeds by dividing generically good inferences into subcases (such as the logically good), and the epistemic story runs at the subcase level.

An illustrative case is Kaplan (1989). His ‘neo-classical consequence’ is classical, in particular: whenever we’ve established p on no premises, we can conclude that □p holds. Kaplan’s ‘logic of demonstratives’ counts more formulae as valid: including contingent formulae like ‘I am here now’. These famously provide counterexamples to the rule of necessitation within the system. Another widely discussed case where more familiar rules are undermined are supervaluational logics, which departs from classical logic only by allowing such moves as the inference from ‘p’ to ‘determinately, p’. But this extension undermines conditional proof, reductio and much else (for discussion, see (Williamson, 1994, ch.5) and Williams (mingb)).
In the case at hand, one might plausibly argue that the move from ‘my experiences are of kind $H$’ to ‘the world satisfies description $T$’ is a priori (albeit defeasibly) truth-preserving (cf. Hawthorne, 2002). But while the inference from $A \Rightarrow C$ to $A \land B \Rightarrow C$ is good when ‘$\Rightarrow$’ is read as expressing logical goodness, it fails for a priori goodness. For example, it is surely not the case that from ‘my experiences are of kind $H$’ and ‘the world doesn’t satisfy description $T$’ it follows a priori that ‘the world satisfies description $T$’.

I think plausible cases can be made for decent patterns of hypothetical reasoning failing on each of the potential generalizations of ‘logical goodness’ we have mentioned. It is beyond the scope of this essay to develop this further.

Of course, I haven’t surveyed all possible attempts. For advocacy of something close to the epistemic irrelevance of logic, see Harman (1988, ch.1.).

The idea is not restricted to the setting of model-theoretic consequence. For example, drawing on recent ‘two-dimensionalist’ treatments of modality, we can characterize a relation sometimes regarded as an explication of a priori entailment by appeal to (centred) worlds which are ‘considered as actual’. In the favoured terminology, we let $\Gamma 1$-entail $B$ if every world that considered as actual is an $A$-world, considered as actual is a $B$ world. Such a characterization of entailment has much in common with Kaplanian validity: that I am here 1-entails that I am here now; but that it is raining now will not 1-entail that it raining at 10am Nov 21st. The discussion that follows could proceed in the material mode in terms of 1-entailment just as well as in the formal mode via Kaplanian validity. As centred worlds are just as fine-grained as contexts (indeed, some contexts with centred worlds) the discussion to follow cold be formulated in this setting.

The Kaplanian definition is a natural generalization of the way the notion of validity is extended to deal with modal languages by parameterizing truth to worlds.

The Kaplan story involves other intricacies. For example, Kaplan develops two different consequence relations, differing in what is held fixed among admissible interpretations. This difference is irrelevant here.

On a language-of-thought model of reasoning, movements in thought from one set of judgements to another fall within this compass.

What of weak invariance, which would require only that the set of contexts not alter the intensions of the sentences. This would not entail stability: so if we could get by with it rather than invariance or constancy in explicating logical good standing, we could avoid the result.

Weak invariance is not a good proposal, I think. For example, imagine the reiteration inference from “dthat(the current president) is a republican” to “dthat(the current president) is a republican”. Suppose this inference is performed across contexts which involve the inauguration of a new republican president. Intuitively, the inference is not in logical good-standing: had a democrat been elected to replace a republican, then the first sentence would be true and the second false. invariance and constancy give this result, for the intension of “the current president” shifts during the course of the argument. But the intensions of the sentence remains the same, so by the lights of a weak invariance criterion, the argument would be in logical good standing.

Lewis (1980) adopts something like this view, based on, among other things, the consider-
The basic ingredients for this story are the account of inference involving demonstratives outlined in Campbell (1994), and its generalization to a wider class of indexical expressions by Prosser (2005). To convert the ‘Fregean’ setting to one amenable to Kaplanian treatment, we can appeal to an account of ‘dynamic words’ based on the treatment of proper names in Kaplan (1990).

Davidson’s truth-theoretic semantic framework, and the structured-proposition theory of Soames (1989), give rise to a finer grained notion of ‘truth-conditions’. I argue elsewhere (Williams, 2008) that the Davidsonian setting prevents us from providing a permutation style proof of overgeneration; and a similar situation arises with the structured proposition framework. The inscrutability problems are merely relocated, however. Developing a theory of how one pairs sentences with fine-grained truth-conditions in such settings is correspondingly harder.

In fact, it is controversial whether ordinary proper names are in category $N$.

I keep the bracketing for notational convenience, though it plays no part of the official definition. It would be a trivial matter to alter the definition of well-formedness to allow for parentheses, but it would be a distraction.

Montague used a richer set of rules within the general semantics itself to make the formal language closer to English syntax. Cf. Partee (1996, §3), Dowty (1979, ch.1) for discussion.

Lewis (1970) includes category $C$ (common nouns) as another basic category, having as appropriate intension a function from indices to sets of objects. For the sake of simplicity, I ignore this here.

Note that there is a single ‘type’ containing all objects—when we define intensional operators over this framework, we will end up with a ‘single domain’ semantics. Plausibly, we want to be able to say that there are things which do exist, which might not exist had some other situation been actual. The solution is to pair each world-index $w$ with a partition of the type of objects into two: those that exist at $w$, and those that do not. We then interpret the ‘ordinary’ loaded existential quantifier relative to $w$ be restricted to those objects that exist at $w$.

This is formulated for derived categories with two elements only. For ‘binary branching’ languages we need no more. For the more general case, we need some additional notation to mark functions from sequences of types to types. (McCawley, 1980, ch.13)

The compositional intensions which Lewis favours differ from the ‘Carnapian intensions’ that form the basic framework for Montague (1970). To characterize a Carnapian intension, one first defines the notion of an appropriate extension in a way paralleling the recursive formulation above. The extension for a name will be an individual of type $o$; the extension for a sentence will be a truth-value of type $t$, and in general an appropriate extension for an expression of category $c/d$ will be of type $\langle \alpha, \beta \rangle$, where $\alpha, \beta$ are the types appropriate to $c, d$ respectively. An appropriate Carnapian intension for an expression of category $Q/R$ will be a function from indices to appropriate extensions, i.e. of type $\langle i, \langle \alpha, \beta \rangle \rangle$ where $\langle \alpha, \beta \rangle$ is the appropriate extension for category $Q/R$. The deficits of a framework based on Carnapian intensions—centrally, its inability to deal with ‘intensional’ expressions such as the predicate ‘is rising’—are discussed in Lewis (1970) and are addressed by Montague by assigning certain expressions semantic values which are not of the Carnapian kind. See Thomason (1974b).
The two settings are equivalent. Given a model that supplies a lexical interpretation $||$, the corresponding compositional valuation is the valuation $v_m$ determined by $||$. Given a model that supplies a compositional valuation, the restriction of that valuation to atomic expressions is the corresponding lexical interpretation. A minor advantage of this setting is that even semantic projection rules are no longer required within the semantic theory, minimizing ‘syncategorematic’ elements that are unmotivated in a metasemantic setting.

Call an assignment of semantic values to sentences coherent if there is at least one compositional valuation that embeds that assignment.

If, following Lewis (1970), we included an extra basic category $C$ (‘common nouns’) mapping indices to sets of objects, then the permuted variant of $|e|$ for $e$ in category $C$ should be $|e| \circ f^1$.

See Lewis (1970, appendix).

Consider, for example, what happens if context changes through the utterance of a sentence say (cf. Lewis, 1979, p.241). So long as we can assume that there’s a unique context associated with each lexical element, context will determine an intension for each such element, which then collectively determine an intension for the whole. The story would be far more complex if we proceed in terms of functions from context-index pairs to truth-values.

For the terminology, see Jackson (1998). For alternative labels (‘secondary intension’ and ‘primary intension’ respectively), see Chalmers (1996). The $C$-intensions also correspond to what Stalnaker (1978) calls the ‘horizontal proposition’ associated with a sentence. Note that $A$-intensions/primary-intensions are not the diagonal propositions of Stalnaker (1978). Stalnaker’s diagonal propositions are not semantic constructs, but are defined pragmatically in terms of agents’ common knowledge of the semantic content of their words.

I set aside concerns about worlds where the individual does not exist.

The terminology would be strictly appropriate if the only variable aspect of context were temporal. Clearly there are many non-temporal ways in which contexts can vary.

This follows from the orthodox treatment of terms as having ‘constant character’, following Kaplan (1989). Some, such as Jackson (1998), claim that the names are indexical. They maintain that, at the least, they can vary depending on what world they are uttered in.
References


McCawley, J. (1980). *Everything that Linguistics have always wanted to Know about Logic (but were ashamed to ask)*. University of Chicago Press, Chicago.


